

## Appendix O

### Assessment of stochastic methods for the thermal design of a telecom satellite

Nicolas Donadey  
(AKKA Technology, France)

Jean-Paul Dudon

Patrick Connil  
(Thales, France)

Patrick Hugonnot

### **Abstract**


The aim of the study is to assess the interest of using probabilistic methods and tools for the thermal design of a telecom satellite. This work has been done in the frame of system development for new satellites.

In the past the interest of such methods compared to deterministic approach leading to use of margin has been pointed locally in the system. It was concluded that these methods are useful to have a more clear and complete exploration of the design and system performances, and thus to identify easily sizing parameters among many inputs. Moreover by associating an occurrence probability to system temperatures related to the dispersion law of relevant input parameters, stochastic approach is expected to avoid a final risky or oversized design.

Here we assess the feasibility of such approach at system level on a telecom satellite by benchmarking probabilistic versus margin method for a S/C communication module. The tools used for this study is OPTIMUS (stochastic methods and computation workflow) and ETHERM (TAS thermal solver)

In this purpose the classical margin approach is compared to a deterministic uncertainty analysis (RMS of cumulative uncertainties on relevant parameters of the thermal design) and to a probabilistic approach (consideration of probabilistic distribution for relevant input parameters).

Methods, tools, and results are presented and current conclusions and perspectives are given considering technical and industrial objectives.




**ThalesAlenia**  
A Thales / Finmeccanica Company *Space*

# Assessment of Stochastic Approach for Thermal Design of a Telecom Spacecraft

*by Nicolas DONADEY (AKKA technology)  
and Jean-paul DUDON, P CONNIL and P HUGONNOT (TAS)*

**28<sup>th</sup> ESA Space Thermal Analysis Workshop  
14-15 oct 2015**

**THALES**  
Thales Alenia Space




**THALES**  
Thales Alenia Space

## SUMMARY

- 1- INTRODUCTION TO STOCHASTIC APPROACH FOR UNCERTAINTY ANALYSIS**
- 2- OBJECTIVES OF THE STUDY**
- 3- METHODOLOGY FOR TELECOM S/C**
- 4- RESULTS**
- 5- CONCLUSION & PERSPECTIVES**

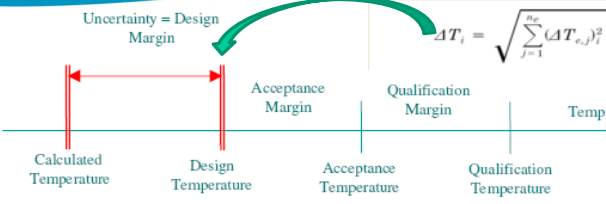
**THALES**  
Thales Alenia Space



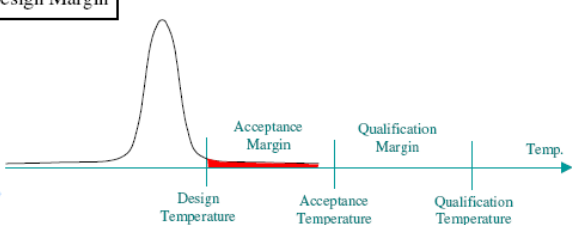
## Thermal Uncertainty Analysis and Stochastic Approach

Page

$$\Delta T_i = \sqrt{\sum_{j=1}^{n_e} (\Delta T_{e,j})^2 + \sum_{k=1}^{n_p} (\Delta T_{p,k})^2 + \sum_{l=1}^{n_t} (\Delta T_{t,l})^2 + \sum_{r=1}^{n_m} (\Delta T_{m,r})^2 + (\Delta T_o)_i}$$



Traditional Approach:  
T Calculated < Design Temperature - Design Margin





Stochastic Approach:  
T Calculated < Design Temperature with a determined confidence level

Design margins with traditional method

Design margins with stochastic method: design to fit with specific probability to remain within limits

**Source : FSASTA ESA study, TAS-I, Blue : Feasibility of Stochastic Approach For Space Thermal Analysis, 2004**

Corporate Communications


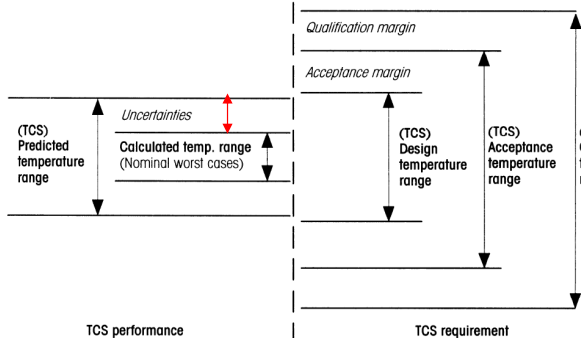


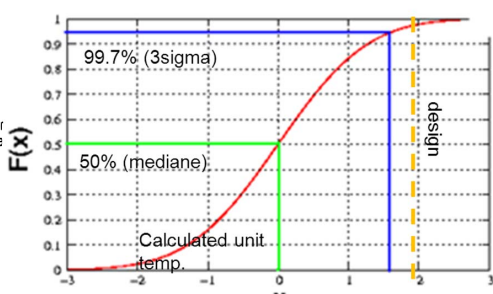
## 2- OBJECTIVES OF THE STUDY


For this study the questions to solve were :

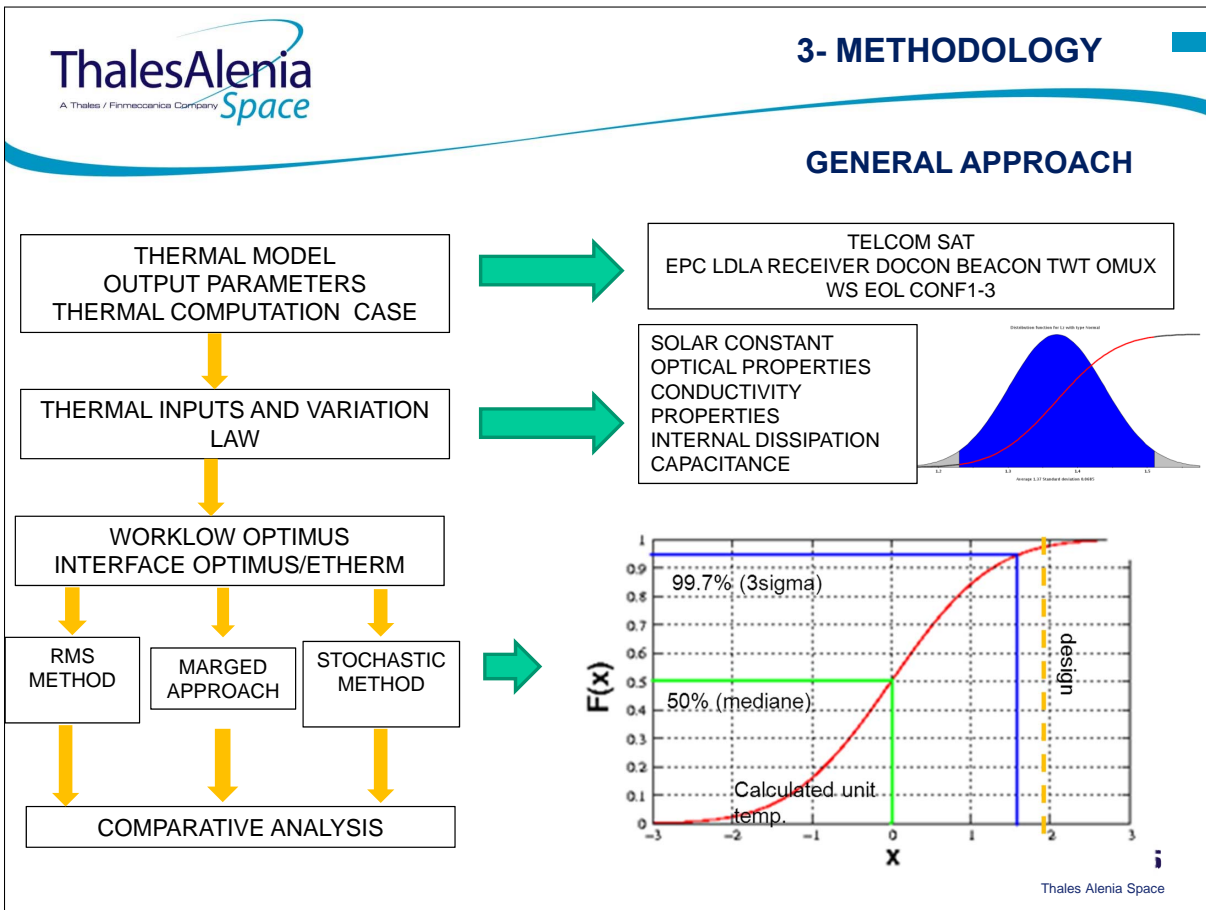
Can we use the stochastic approach to assess the thermal design of a telecom spacecraft ?

Does it lead to a margin reduction and an increase of competitiveness compared to the margin approach ?









**ThalesAlenia Space**  
A Thales / Finmeccanica Company

### 3- METHODOLOGY

#### MODEL DESCRIPTION

For the study we selected the thermal model TELCOM SAT that was correlated with thermal vacuum test results.  
Configuration case chosen : WS EOL CONF 1-3 (worst case with regard to our goal) .

In order to minimize the data volume, we focused on one of both CM N/S panels. But results shall be similar for the other one.

		Nomenclature		Trp	
PAYLOAD	South CM	Top 65°C	EPC	1EP403 (middle)	4766
			LDLA	1CL2-08 (+x)	4786
		Bottom 85°C	RECEIVER	1RE3-05	4707
			DOCON	1DC1-03	4704
			BEACON	1BE2-01	4844
			TWT	1TE403A (+x)	4694
	Top 85°C	OMUX	1MS502(Northern)	4140	
		TWT	1TE309B (-x)	4574	
	Bottom 65°C	OMUX	1MS401 (Russian)	4145	
		EPC	1EP307 (-x)	4762	
			LDLA	1CL2-09 (--x)	4796

**TELCOM SAT CM SELECTED OUTPUT DATA**

**TELCOM CM Configuration 1-3**

Legend for Configuration 1-3:

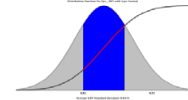
- Input section units
- PLDIU unit
- ⌘Saturation
- @Saturation
- ⊙Saturation
- ⊚Saturation

**THALES**  
Thales Alenia Space

COMPUTATION HYPOTHESIS

Dispersion law for inputs (range and form) taken from :

- ECSS-E-30-PART 1A : min/max range
- Doc 02,07,035/TN5 p226 (FASSTA study for ESA 2004) : law type
- Internal TAS applicable documents for thermal control (modeling error=2°C)



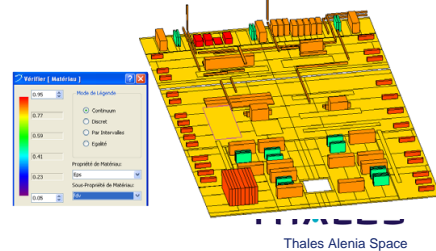
Variable inputs are grouped by type of coating, by material, by type of contact, ...

The attached variation law is operated in the same way to all inputs of each group

- Ex: All the EPC surfaces have an emissivity equal to 0.85. If this value change from 0.85 to 0.86, each EPC will have an emissivity of 0,86
- Ex2 : All dissipations of the CM module are also varied in the same rate

		WS EOL 100% Drive			
		CONF 1-3			
		Tmax	Nomenclature	Trp	
PAYLOAD South CM	Top 65°C	EPC	44.7	1EP403 (middle)	4766
		LDLA	44.3	1CL2-08 (+x)	4786
		RECEIVER	45.2	1RE3-05	4707
		DOCON	44.9	1DC1-03	4704
		BEACON	42.4	1BE2-01	4844
	Top 85°C	TWT	60.7	1TE403A (+x)	4694
		OMUX Northern (6ch)	54.4	1MS502(Northern)	4140
	Bottom 85°C	TWT	59.4	1TE309B (-x)	4574
		OMUX Russia (9ch)	56	1MS401 (Russian)	4145
	Bottom 65°C	EPC	32.5	1EP307 (-x)	4762
		LDLA	29.97	1CL2-09 (-x)	4796

VIEW OF ETHERM RADIATIVE MODEL OF THE PANEL WITH UNITS



TELCOM SAT CM NOMINAL TEMPERATURE FOR CONSIDERED UNITS

THERMAL INPUT PARAMETERS

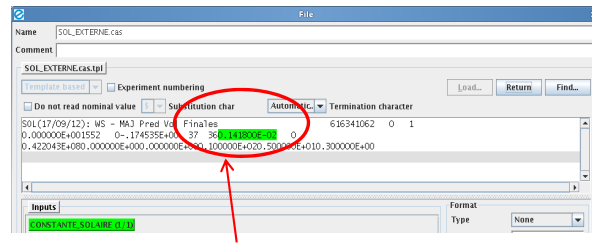
			SIGMA (Loi gaussienne) Doc 02,07,035/TN5 p226				INCERTITUDE ECSS-E-30-PART 1A			Affectation			
			Valeur nominale	Loi de variation	(%)	Sigma	%	Fixe	Borne min		Borne max		
CONDUCTIF	PANNEAU CM	Lx Ly	3,81	Normal	5	0,1905	10		3,43	4,19	Fichier cas de calcul plateau		
		Lz	1,37	Normal	5	0,0685	10		1,23	1,51			
	CONDUCTANCE CONTACT	Heat-pipe/Structure1	933,00	Normal	25	233,2500	25		700	1166	Table gopi 41		
		Heat-pipe/Structure2	2400,00	Normal	25	600,0000	25		1800	3000			
		Unit/Aluminium	1200,00	Normal	25	300,0000	25		900	1500			
		Heat-pipe/Xing	5000,00	Normal	25	1250,0000	25		3750	6250			
		Unit/Heat-pipe	5000,00	Normal	25	1250,0000	25		3750	6250			
coeff*	1,00	Normal	25	0,2500	25		0,75	1,25	Table CONDHP 241				
RADIATIF	INTERNE	Eps CAMP	0,50	Normal	5	0,0250		0,03	0,47	0,53	Table alvéole interne 628		
		Eps E D R O (Eps_085)	0,85	Normal	5	0,0425		0,03	0,82	0,88			
		Eps Z307_BEACON (Eps_Z307)	0,95	Normal	5	0,0475		0,03	0,92	0,98			
		Eps Z306_TWT (Eps_Z306)	0,90	Normal	5	0,0450		0,03	0,87	0,93			
		Eps NIDA	0,80	Normal	5	0,0400		0,03	0,77	0,83			
		Eps MLI (Eps1_MLI)	0,05	Normal	5	0,0025		0,02	0,03	0,07			
		Beq MLI (W/°C.mm²)	1,0000E-07	Normal	15	0,000000015	50		5,00E-08	1,50E-07		Table appel 2624	
	Eps_eq MLI	0,0050	Normal	15	0,0008	50		2,50E-03	7,50E-03				
	EXTERNE	Alp OSR	Alp OSR	0,255	Normal	5	0,0128		0,03	0,23	0,29	Table alvéole externe 1062	
			Eps OSR	0,84	Normal	5	0,0420		0,03	0,81	0,87		
			Eps TWT	0,80	Normal	5	0,0400		0,03	0,77	0,83		
			Alp TWT	0,70	Normal	5	0,0350		0,03	0,67	0,73		
			Eps MLI	0,84	Normal	5	0,0420		0,03	0,81	0,87		
		Alp MLI	Alp MLI	0,93	Normal	5	0,0465		0,03	0,90	0,96		
			Beq MLI (W/°C.mm²)	2,0000E-08	Normal	15	0,000000003	50		1,000E-08	3,000E-08		Table appel 2624
			Eps_eq MLI	0,0109	Normal	15	0,0016	50		5,430E-03	1,629E-02		
			EXTERNE	Constante solaire	1418,00	Normal	10	141,8000		21,00	1397		1439
CAPACITANCE				Cp	Equipement	1,00	Normal	5	0,0500	25			0,75
	Structure	1,00	Normal		5	0,0500	15		0,85	1,15			
PUISSANCE	CM	Table Puissance	1,00	Uniforme		0,0000	5		0,95	1,05	Table 1893 *		
		Table Harness	1,00	Uniforme		0,0000	5		0,95	1,05	Table 1888 *		
TOTAL			25										

Brief presentation of OPTIMUS tool (by NOESIS)

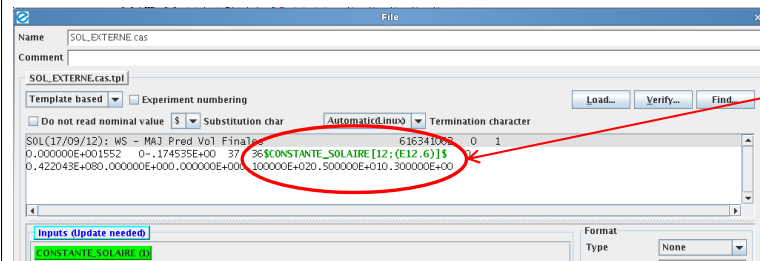
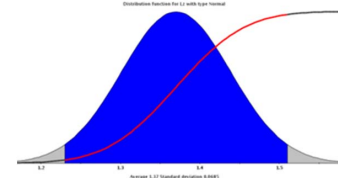
For this study, OPTIMUS tool was used to manage and automatize all the computation process & to perform the stochastic analysis

Typically OPTIMUS allows to :

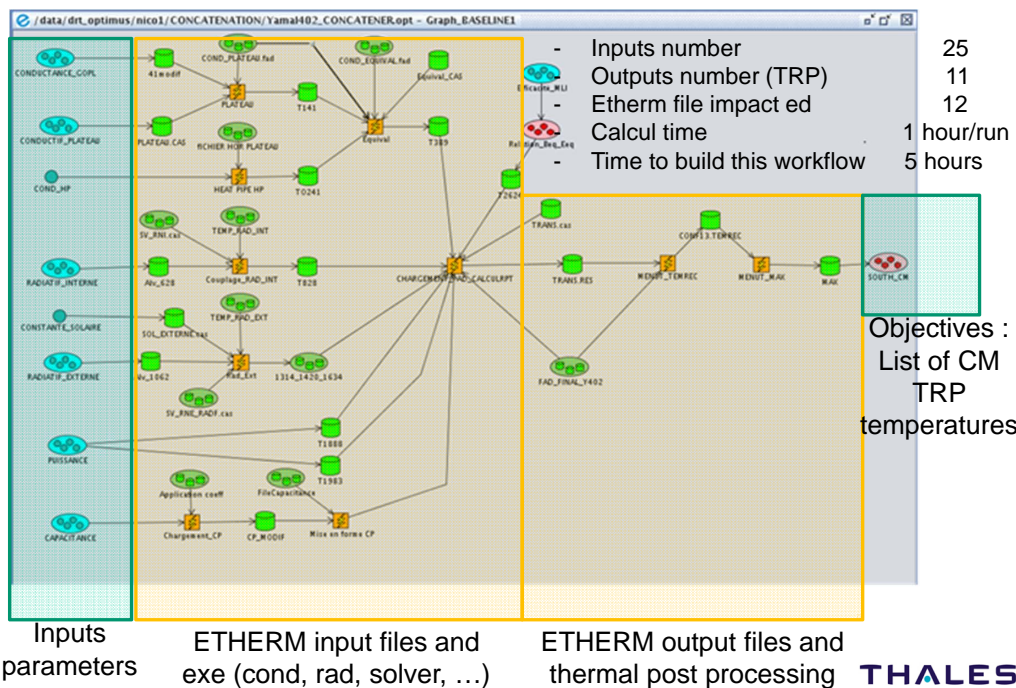
- Attach probabilistic distributions to inputs
- Launch all required calculation cases (including parallel run capability) on any thermal tools (ETHERM here)
- Use many powerful stochastic & deterministic methods for model exploration, uncertainty & sensitivity and for optimisation (DOE, RSM, MCS, global optimisation,...)
- Post-process all results in an ergonomic and rapid way (table, graphics, ...)



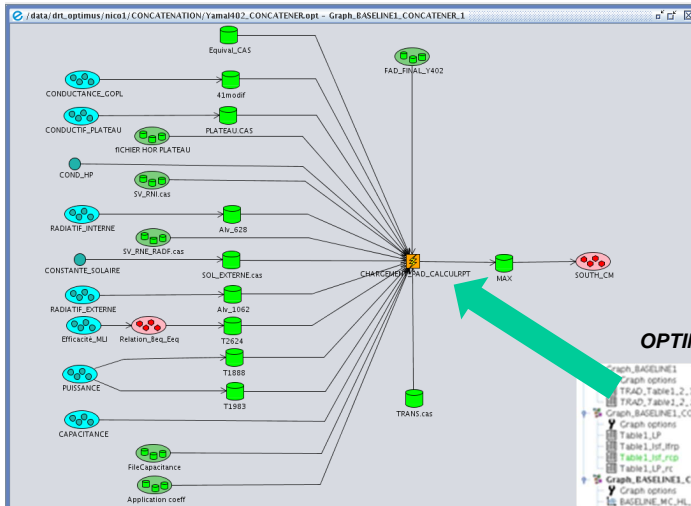
Via Optimus, the input parameters are changed as a variable. The user can choose a different probabilist law for each parameter.



OPTIMUS WORKFLOW with ETHERM thermal tool

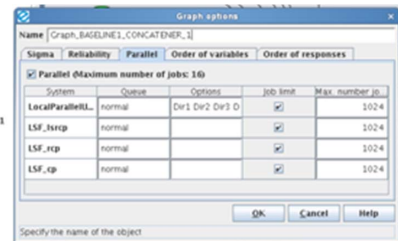


OPTIMUS WORKFLOW for parallel computations



In order to optimize the computation time a parallel workflow was built to run 16 cases at a time  
 In nominal condition, **1000 computations are performed in 3 days for the whole CM model**

OPTIMUS option box for parallel computation



TRADITIONAL METHOD VS STOCHASTIC METHOD

TRADITIONAL APPROACH  
 Root Mean Square (RMS)

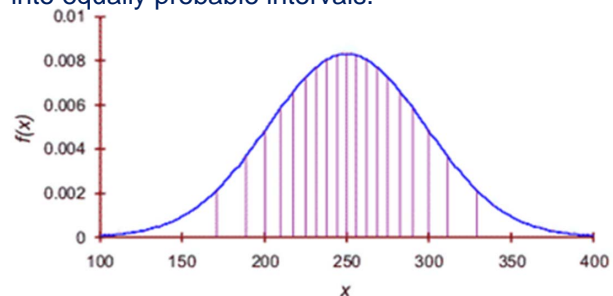
- The traditional approach to determine uncertainty is a root mean square :
- We consider each parameter one by one as input
- For each run, all the parameters have their nominal value except the current one which have his worst value.
- For each unit the global temperature uncertainty is defined as :


$$\Delta T_{unit}^{RMS} = \sqrt{\sum_k^{25} \Delta T_k^2}$$

with  $\Delta T_k = T_{unit\ calc. with\ nominal\ value\ of\ parameter\ k} - T_{unit\ calc. with\ worst\ value\ of\ k}$

STOCHASTIC APPROACH  
 MONTE CARLO WITH LATIN HYPERCUBE

MCS : N samples (N=1000) of K variables (K=25) are randomly produced and the thermal model is run N times with these samples.  
 Latin hypercube sampling (LHS) is a statistical method used to optimize efficiency of MCS and respect the initial distribution (gaussian, truncated or uniform). The range of each variable is divided into equally probable intervals.





## 4- RESULTS

### RMS uncertainty analysis results

**25 parameters**      **11 units** →

Element	PAYLOAD											
	Top 65°C					South GM			Bottom 85°C			Bottom 65°C
Nomenclature	EPC	LDLA	RECEIVER	DOCON	BEACON	TWT	OMUX(Northern (sch))	TWT	OMUX(Russia (sch))	EPC	LDLA	
Trip	4766	4786	4707	4704	4844	4684	4140	4574	4145	4762	4796	
Transmiter	44,7	44,26	45,33	44,91	42,51	60,72	54,43	58,46	56,01	32,8	30,01	


  


Element	PAYLOAD											
	Top 65°C					South GM			Bottom 85°C			Bottom 65°C
Nomenclature	EPC	LDLA	RECEIVER	DOCON	BEACON	TWT	OMUX(Northern (sch))	TWT	OMUX(Russia (sch))	EPC	LDLA	
Trip	0,17	0,35	0,24	0,23	0,16	0,43	0,43	0,48	0,47	0,09	-0,10	
Transmiter	0,25	0,38	0,26	0,26	0,28	0,53	0,55	0,54	0,55	0,22	0,24	
	-0,02	0,00	-0,03	-0,02	-0,03	0,06	0,06	0,05	0,06	0,00	0,01	
	0,08	0,03	0,06	0,08	0,05	0,01	0,01	0,01	0,00	0,06	0,03	
	0,19	0,28	0,38	0,33	0,20	0,00	0,00	0,00	0,00	0,17	0,15	
	0,42	-0,21	0,08	0,25	-0,04	0,92	-0,47	0,39	-0,08	0,51	0,01	
	0,00	0,06	0,00	0,01	0,00	0,00	0,00	0,00	0,00	0,00	0,01	
	-0,03	-0,01	-0,03	-0,03	-0,01	0,00	0,00	0,00	-0,01	-0,03	0,00	
	0,00	0,00	0,00	0,01	0,00	0,00	0,00	0,00	0,00	0,00	0,00	
	0,00	0,00	0,00	0,00	0,00	0,00	0,00	-0,01	0,00	0,00	0,00	
	0,02	0,04	0,01	0,02	0,02	-0,01	-0,01	0,00	0,00	0,00	0,01	
	0,06	0,06	0,05	0,07	0,05	-0,11	-0,12	-0,12	-0,13	0,06	0,06	
	0,06	0,06	0,05	0,07	0,05	-0,09	-0,10	-0,09	-0,10	0,06	0,07	
	2,54	2,52	2,54	2,54	2,62	2,62	2,69	2,61	2,69	2,57	2,73	
	2,05	2,04	2,04	2,04	2,11	2,24	2,30	2,21	2,30	1,83	1,98	
	0,03	0,03	0,03	0,03	0,03	0,21	0,15	0,21	0,15	0,02	0,04	
	0,01	0,01	0,01	0,01	0,01	0,07	0,05	0,07	0,05	0,00	0,02	
	-0,01	-0,01	-0,01	-0,01	-0,01	-0,02	-0,02	-0,02	-0,02	-0,01	0,00	
	0,01	0,01	0,01	0,01	0,01	0,01	0,02	0,01	0,01	0,01	0,01	
	0,00	-0,01	0,00	0,00	0,01	0,02	0,02	0,01	0,01	-0,01	0,01	
	0,37	0,37	0,36	0,37	0,37	0,39	0,38	0,38	0,37	0,38	0,39	
	0,01	0,00	0,00	0,01	0,01	0,00	0,02	0,03	0,01	0,01	0,02	
	0,02	0,01	0,01	0,02	0,02	0,00	0,00	0,01	0,00	0,02	0,02	
	2,43	2,39	2,45	2,44	2,36	3,03	2,82	2,97	2,91	1,86	1,85	
	0,01	0,02	0,01	0,02	0,01	0,01	0,01	0,01	0,01	0,01	0,07	
<b>RMS</b>	<b>4,13</b>	<b>4,09</b>	<b>4,13</b>	<b>4,13</b>	<b>4,14</b>	<b>4,75</b>	<b>4,62</b>	<b>4,63</b>	<b>4,66</b>	<b>3,73</b>	<b>3,88</b>	

Prise en compte de l'erreur modèle (2°C)	RMS 2°C											
	2	2	2	2	2	2	2	2	2	2	2	
<b>Total RMS error for each unit</b>	<b>4,58</b>	<b>4,56</b>	<b>4,59</b>	<b>4,59</b>	<b>4,59</b>	<b>4,60</b>	<b>5,16</b>	<b>5,04</b>	<b>5,04</b>	<b>5,07</b>	<b>4,23</b>	<b>4,37</b>
<b>RMS 2°C - RMS (pour étude stochastique)</b>	<b>0,46</b>	<b>0,46</b>	<b>0,46</b>	<b>0,46</b>	<b>0,46</b>	<b>0,40</b>	<b>0,41</b>	<b>0,41</b>	<b>0,41</b>	<b>0,50</b>	<b>0,49</b>	

A highly automated computation process that gives RMS uncertainty & confirms the list of influent parameters issued from RSM contribution (CM dissipations,  $\alpha_{OSR}$ ,  $\epsilon_{OSR}$ )





## 4- RESULTS

### Stochastic uncertainty analysis results

#### Glossary

**Cumulative distribution function (CDF)**  
 The cumulative distribution function describes the probability for the unit temperature to have a value less than or equal to a limit (nominal, design, acceptance, ...)

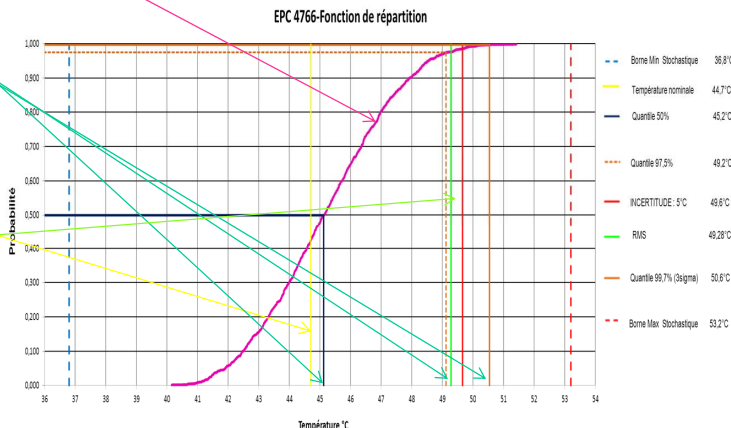
**Quantiles (50% / 97.5% / 99.7%)**  
 Quantile are points taken at regular intervals from the CDF.  
 99.7% quantile correspond to 3sigma design

**Nominal temperature**  
 Temperature calculated when all the parameter have their nominal value.

**RMS Temperature**  
 Temperature error obtained with RMS method considering the accumulation of effect of all the input parameters of the study (added to nominal temp)


**Uncertainty margin 5°C : Tnominal +5°C**

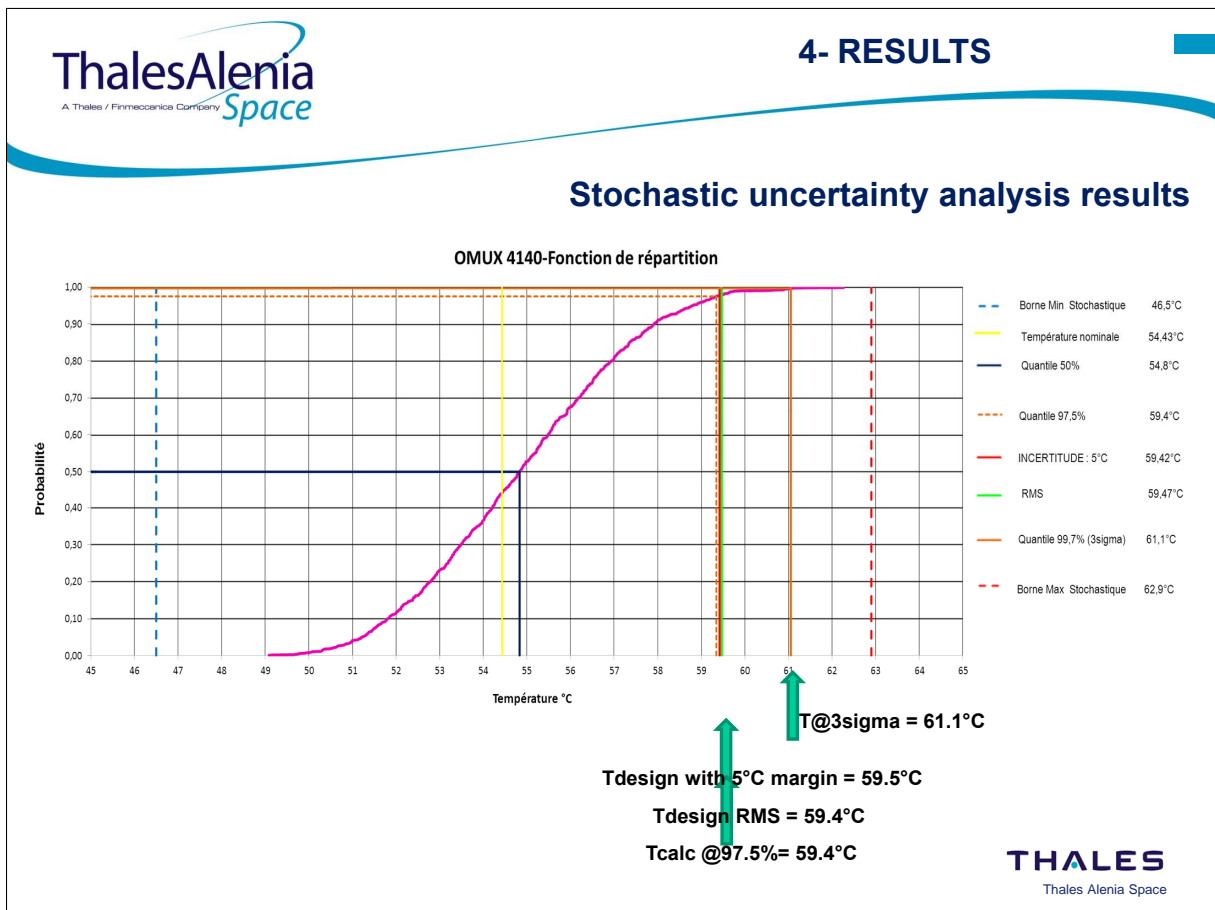
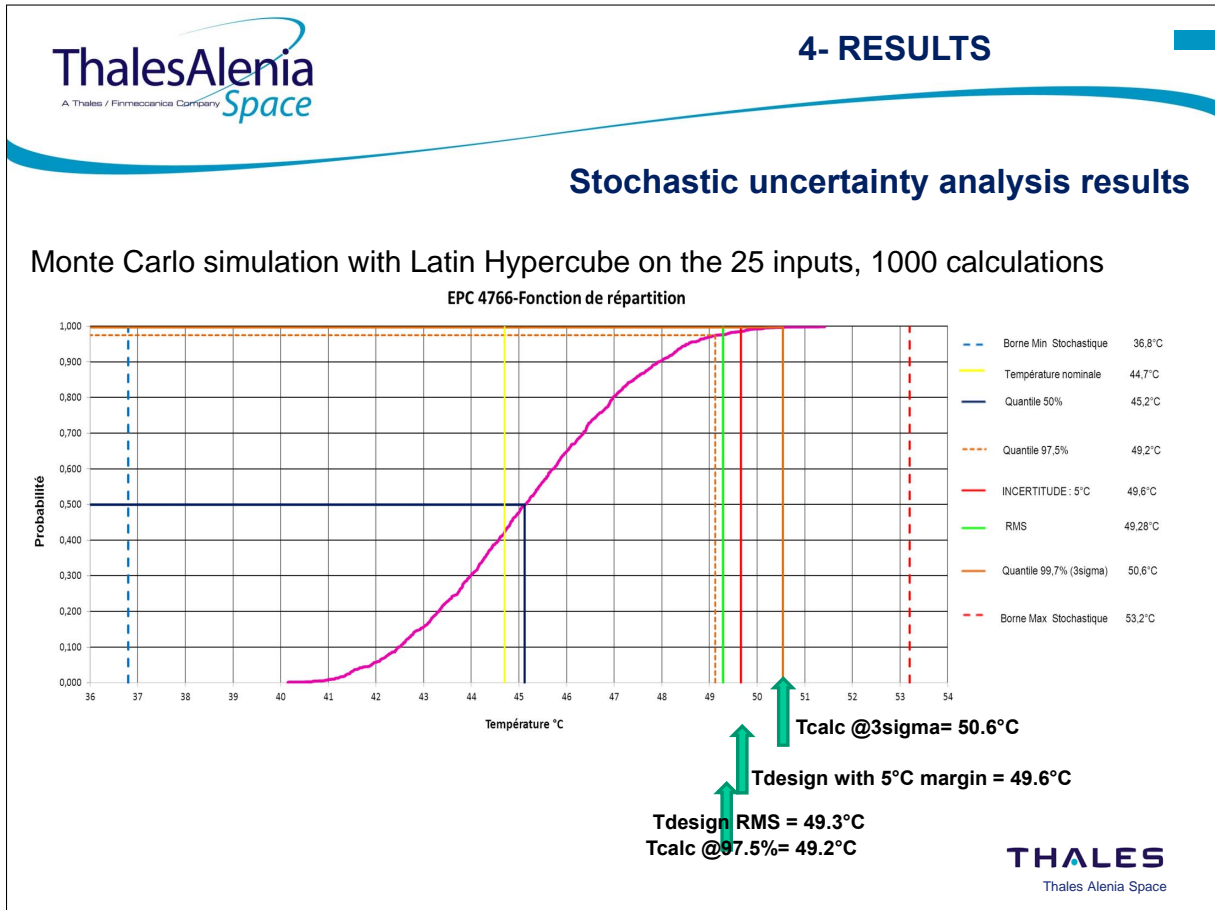
**Boundary temperature (min and max)**  
 The lowest and highest temperature obtained over the 1000 runs

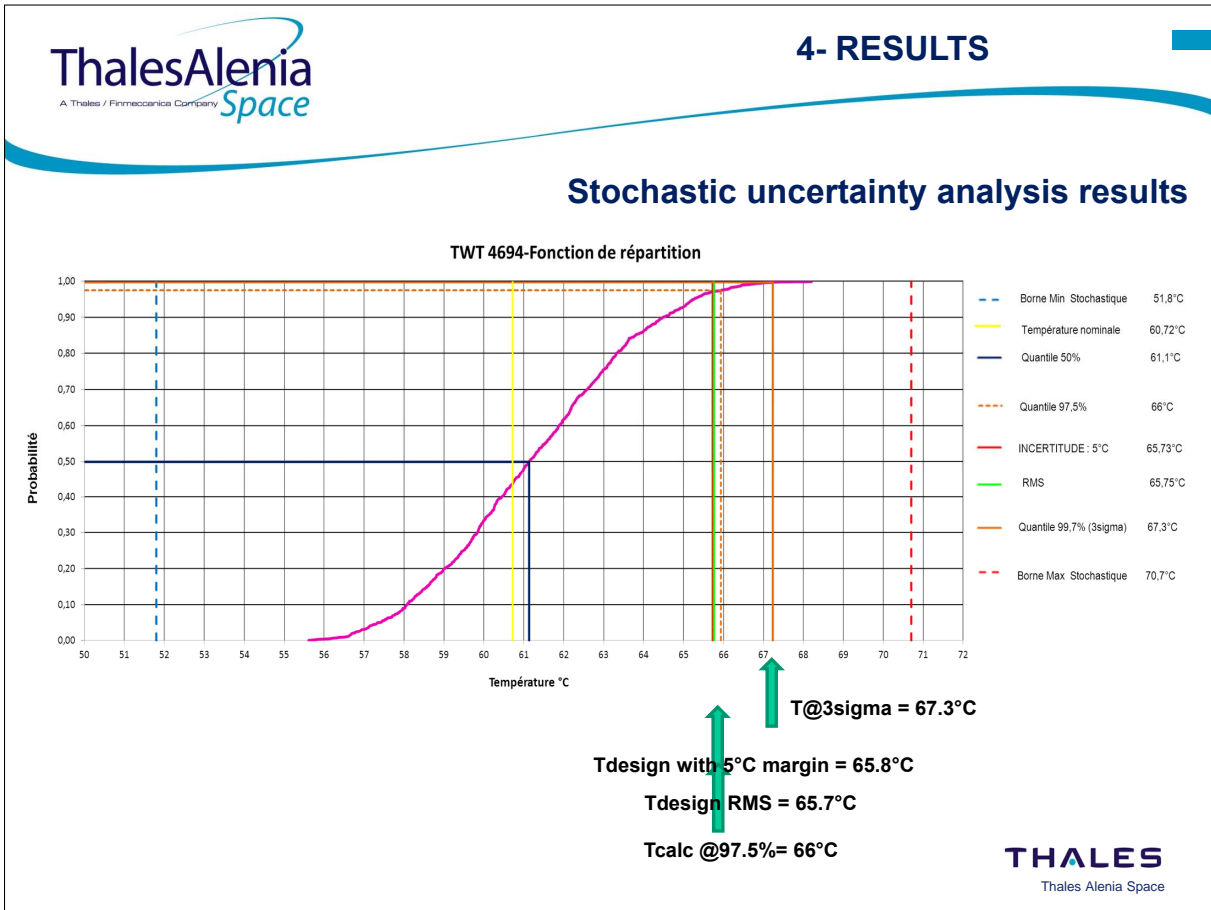


EPC 4766-Fonction de répartition

Line Style	Value
Blue dashed	Borne Min Stochastique 36,8°C
Yellow solid	Température nominale 44,7°C
Blue solid	Quantile 50% 45,2°C
Orange dashed	Quantile 97,5% 49,2°C
Red solid	INCERTITUDE: 5°C 48,6°C
Green solid	RMS 49,28°C
Orange solid	Quantile 99,7% (3sigma) 51,6°C
Red dashed	Borne Max Stochastique 53,2°C







**4- RESULTS**

### SUMMARY OF RESULTS

INCERTITUDE CALCUL MODELE YAMAL 402 CONFIGURATION: WS EOL 100% Drive CONF 1-3

	Nomenclature	Trp	Tnominal °C	TRADITIONELLE		STOCHASTIQUE (T en °C)								
				Incertitude: + 5°C	RMS T °C DT	50% (médian)		97.5% ( )		99% (3sigma)				
						T Calculé	Ecart (Tc-Tston)	T Calculé	Ecart (Tc-Tn)	T Calculé	Ecart (Tc-Tn)			
SOUTH CW	Top 85°C	EPC	1EP403 (middle)	4766	44,7	49,7	49,3	4,6	45,2	0,5	49,2	4,5	50,6	5,9
		LDLA	1CL2-08 (+x)	4786	44,3	49,3	48,9	4,6	44,8	0,5	48,6	4,3	50,2	5,9
		RECEIVER	1RE3-05	4707	45,3	50,3	49,9	4,6	45,8	0,5	49,9	4,6	51,2	5,9
		DOCON	1DC1-03	4704	44,9	49,9	49,5	4,6	45,4	0,5	49,5	4,6	50,8	5,9
		BEACON	1BE2-01	4844	42,5	47,5	47,1	4,6	43,0	0,5	46,9	4,4	48,5	6,0
PAYLOAD	Top 85°C	TWT	1TE403A (+x)	4694	60,7	65,7	65,9	5,2	61,1	0,4	66,0	5,3	67,3	6,6
		OMUX Northern	1MS502(Northern)	4140	54,4	59,4	59,4	5,0	54,8	0,4	59,4	5,0	61,1	6,7
		TWT	1TE309B (-x)	4574	59,5	64,5	64,5	5,0	59,9	0,4	64,5	5,0	66,0	6,5
Bottom 85°C	OMUX Russia	1MS401 (Russian)	4145	56,0	61,0	61,1	5,1	56,4	0,4	61,0	5,0	62,6	6,6	
	Bottom 65°C	EPC	1EP307 (-x)	4762	32,9	37,9	37,1	4,2	33,4	0,5	37,0	4,1	38,1	5,2
	LDLA	1CL2-09 (-x)	4796	30,0	35,0	34,3	4,4	30,5	0,5	34,2	4,2	35,6	5,6	

The first target of the study is reached : probability was associated to calculated unit temperatures within a telecom system by taking into account uncertainties on inputs. It points out that :

**DT RMS ≈ DT stochastic @97.5% ≈ 5°C = design margin ≈ DT@3sigma**

➔ In this case the stochastic approach does not allow to reduce the usual margin of 5°C.

**THALES**  
Thales Alenia Space

Globally this study pointed out the following major conclusions :

- Feasibility of intensive sensitivity analysis of a telecom thermal model at low computation cost with OPTIMUS (not presented)
  - Feasibility to associate reliable probability distributions to unit temperatures using the same workflow than for sensitivity (1000 runs thanks to parallel mode)
  - This approach did not allow to reduce the usual margin of 5°C for the design,
  - However it pointed out that this margin currently in use for design is
    - in agreement with RMS « exhaustive » computation
    - Is overpassed in less than 2 % of cases (by less than 2°C)
- With the current margin the thermal design is conservative, but not clearly oversized !
- OPTIMUS process was optimized :
    - Better interface OPTIMUS/Etherm
    - Possibility to execute lots of runs in parallel (more than 1000 runs at all).

**Complete the first probabilist approach on CM** by taking into account the uncertainty on spatial distribution for dissipations and for P/L failure cases (TBC)

**Improve and optimize OSR area (on going)**

- Optimisation methods and automated workflow capability
- Sensible saving expected on analysis duration

**Telecom S/C model correlation (on going)**

- Model exploration, Optimisation methods, automated workflow capability
- **Particular interest targeted** : performing correlation and flight prediction in a same coupled computation process (weeks of saving expected)