#### **Appendix L**

#### General-purpose GPU Radiative Solver

Andrea Tosetto Marco Giardino Matteo Gorlani (Blue Engineering & Design, Italy)

#### Abstract

In the scope of the CADET project, a new radiative tool was developed in Blue Engineering. The tool can compute the extended view-factor and extended incident heat fluxes for solar, planetary and albedo contributions using the Monte Carlo Ray Tracing model. The software is implemented using the OpenCL framework, in order to take advantage of the computational capabilities of GPGPU hardware and dedicated computation hardware.

A comparison between tool results and ESATAN TMS results is performed in order to validate the tool.





### **CADET Project**

- CApture and DE-orbiting Technologies
- Develop enabling technologies required for Active Debris Removal from LEO orbits:
  - IR and Visible tracking of the target
  - Develop GNC for close rendez-vous, final approach and capture phases
  - technologies, strategies and concepts for target capture and solidarization
- BLUE contribution: <u>onboard</u> IR image processing to get target relative position and motion, with simplified thermal analysis (low power HW)

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## Radiative heat exchange

Radiation exchange	Heat fluxes
View Factor F <sub>ij</sub> : fraction of the radiant energy emitted by surface <i>i</i> <u>directly</u> <u>intercepted</u> by surface <i>j</i> ;	<b>Direct incident heat fluxes</b> : radiative energy emitted by an external source <u>directly intercepted</u> by a surface;
Radiative exchange factors (REF, also Gebhart factors) B <sub>ij</sub> : fraction of the radiant energy emitted by surface <i>i</i> <u>finally</u> <u>absorbed</u> by surface <i>j</i> (including surfaces diffuse reflections);	<b>Total absorbed heat fluxes</b> : radiative energy emitted by an external source <u>finally absorbed</u> by a surface (including diffuse reflection component);
<b>Extended view factors F</b> <sub>ij</sub> : fraction of the radiant energy emitted by surface <i>i</i> <u>finally</u> <u>absorbed</u> by surface <i>j</i> , directly of through diffuse or specular reflections and through transmissions; $\rightarrow$ <b>GR (also REF)</b>	<b>Extended incident heat fluxes</b> : radiative energy emitted by an external source <u>finally absorbed</u> by a surface, directly of through diffuse or specular reflections and through transmissions;
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# Why GPGPU?

- Rendering real life pictures is quite similar to evaluate heat fluxes and view factors
- GPU are made for rendering
- Modern GPU are programmable for general purpose calculations using CUDA or OpenCL programming languages (most mature and common)
- GPU are powerful: CPUs ~10GFLOPS, GPUs ~5TFLOPS
- GPU consume less power per GFLOPS (mobile GPUs ~4watts)

General-Purpose computing on Graphics Processing Units (GPGPU) → using GPU hardware to perform computations



	GPGPU	- history								
General	•Purpose computing on G → using GPU hardware	raphics Processing Units to perform computations	(GPGPU)							
Dedie     opera     scene	cated graphic hardware ation on huge data sets in es	evolved aiming to boost order to render more det	t simple ailed CG							
<ul> <li>From progr</li> </ul>	2002 (NVIDIA GeForce 3, rammable rendering pipel	ATI Radeon 9700): introdu ine (Direct3D 8.0, OpenGL	uction of . 1.4)							
<ul> <li>Dedicomposition</li> </ul>	cated languages enabled outations:	GPU processors to be	used for							
	CUDA, 2007	OpenACC, 2012								
	OpenCL, 2009 C++ AMP, 2012									
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GPGPU – structure (2)							
	CPU	GPU					
Architecture	MIMD (Multiple Instruction Multiple Data) → Multi purpose, independent processors/cores	SIMD (Single Instruction Multiple Data) $\rightarrow$ 1 control unit dispatch commands to multiple ALUs. Texture units					
Execution	Branch execution flow, control structures	Optimized for branchless execution (maximize occupancy)					
Memory structure	<ul> <li>Low latency, low bandwidth memory (RAM, up to 20 GB/s)</li> <li>L1, L2, L3 levels cache memory</li> <li>CPU registers</li> </ul>	<ul> <li>High latency, high bandwidth memory (VRAM, up to 300 GB/s)</li> <li>On chip, block shared memory</li> <li>GPU registers</li> </ul>					
Memory management	Automatic (e.g. cache pre-fetch)	User controlled data flow between VRAM and shared memory, registers					
Context switch	Software (thread management by OS)	HW (thread switch controlled by the control unit to hide memory latency)					
Precision	Single, double, quad, with almost same performances	Preferred single, double available but with <u>huge performance</u> losses (at best, ¼ of single precision on latest hardware)					
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# GPGPU Programming languages

CUDA	OpenCL
GPGPU language by NVIDIA	Open standard by Khronos Group (OpenGL)
Specific and available only on NVIDIA GPUs	Designed for heterogeneous computing: available on NVIDIA and AMD GPUs, ARM processors, CPUs (Intel & AMD), FPGA vendors
Offline kernel compilation to intermediate language	Runtime kernel compilation of the provided kernel sources by the device specific driver
Mature framework, with libraries (CuFFT, CuBLAS, etc.) and tools (IDE, profiler, debugger, etc.)	Less advanced libraries and tools, generally from open source projects
Work only on NVIDIA hardware	The standard guarantee software portability among different HW (NB execution performances are not guaranteed: they can only be achieved tuning software on each specific hardware architecture)
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## GPGPU Platform (OpenCL dialect)

Host (CPU)	Device (GPU, FPGA, etc)
Host code: C, C++, Fortran, C#, Java, Python, ecc.	Device code (kernels): OpenCL C, which is a modified C99 (add vector primitives and vector functions; some restrictions in use of pointers, some standard C99 headers are missing)
Manage the algorithm workflow	Perform computations on the provided data sets
Manage the data transfer between host memory (RAM) and device memory (VRAM); memory can be a shared area between host and device	Manage data flow among device mass memory, device shared memory and processor registers, through kernel's instructions
Manage global execution synchronization	Execution is divided in 1D, 2D or 3D workgroups; block synchronization can be obtained through device shared memory
Host code controls the para	llel execution of dedicated kernels on els are compiled during initialization



#### **Computer Graphics Rendering Heritage**

- Rasterisation → objects lightning obtained through artifacts (textures)
- Global illumination → direct evaluation of an objects appearance, due to objects and light sources positions, object properties, etc
- Ray Tracing Monte Carlo (RTMC)

   → Elegant solution to compute global illumination, under development from 1980s [Kay & Kajiya 1986]



[Fabianowski 2011]











## Open Box test – Earth flux results

Node	10	11	20	21	30	31				
CADET	153.7860	6.7952	43.1359	11.6836	42.5930	10.3962				
ESATAN	153.6489	6.9998	42.6820	11.4758	42.3568	10.1615				
Abs. err.	0.137070	-0.204551	0.453887	0.207798	0.236169	0.234655				
Rel. Err. %	0.089209	2.922240	1.063411	1.810749	0.557570	2.309245				
Node	40	41	50	51	60	61				
CADET	0	34.9459	42.9083	11.7025	42.9015	42.9358				
ESATAN	0	35.0538	42.9592	11.4846	42.6880	42.7810				
Abs. err.	0	-0.107996	-0.050915	0.217839	0.213462	0.154752				
Rel. Err. %	0	0.308085	0.118519	1.896782	0.500051	0.361730				
NB due to	o the selected	l attitude, Ear	rth fluxes are	the same on	each point of	the orbit				
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## Open Box test – Sun flux results

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Tot

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P1	0.00	0.00	0.00	0.00	1000.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	1000.00
P2	0.00	0.00	0.00	0.18	923.88	0.00	382.68	0.00	0.00	0.09	0.00	0.00	1306.84
<b>P3</b>	0.00	0.00	0.00	0.00	707.11	0.07	707.11	0.14	0.00	0.00	0.00	0.00	1414.43
P4	0.00	0.00	0.00	0.00	382.68	0.04	923.88	0.08	0.00	0.00	0.00	0.00	1306.68
Р5	0.00	0.00	0.00	0.00	0.00	0.00	1000.00	0.00	0.00	0.00	0.00	0.00	1000.00
P6	0.00	0.09	0.00	0.18	0.00	0.09	923.88	0.09	0.00	0.00	382.68	0.18	1307.21
P7	0.00	0.28	0.00	0.14	0.00	0.42	707.11	0.57	0.00	0.35	707.11	0.07	1416.05
P8	0.00	0.28	0.00	0.28	0.00	0.26	382.68	0.50	0.00	0.22	923.88	0.09	1308.19
P9	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	1000.00	0.00	1000.00
_													
	10	11	20	21	30	31	40	41	50	51	60	61	Tot
P1	-0.05	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
P2	0.00	0.00	0.00	0.18	-0.02	0.00	0.00	0.00	0.00	0.09	0.00	0.00	0.26
<b>P3</b>	0.00	0.00	0.00	0.00	-0.02	0.07	0.00	0.14	0.00	0.00	0.00	0.00	0.19
P4	0.00	0.00	0.00	0.00	-0.02	0.04	0.00	0.08	0.00	0.00	0.00	0.00	0.10
P5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
P6	0.00	0.09	0.00	0.18	0.00	0.09	0.00	0.09	0.00	0.00	-0.02	0.18	0.63
<b>P7</b>	0.00	0.28	0.00	0.14	0.00	0.42	0.00	0.57	0.00	0.35	-0.02	0.07	1.81
P8	0.00	0.28	0.00	0.28	0.00	0.26	0.00	0.50	0.00	0.22	-0.02	0.09	1.61
					0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.05
P9	-0.05	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
P9	-0.05	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
	P1 P2 P3 P4 P5 P6 P7 P8 P9 P1 P2 P3 P4 P5 P6 P6 P7	P1         0.00           P2         0.00           P3         0.00           P4         0.00           P5         0.00           P6         0.00           P7         0.00           P8         0.00           P9         0.00           P1         -0.05           P2         0.00           P3         0.00           P4         0.00           P3         0.00           P4         0.00           P5         0.00           P5         0.00	P2         0.00         0.00           P2         0.00         0.00           P3         0.00         0.00           P4         0.00         0.00           P5         0.00         0.00           P6         0.00         0.00           P7         0.00         0.28           P8         0.00         0.28           P9         0.00         0.00           P2         0.00         0.00           P3         0.00         0.00           P4         0.00         0.00           P3         0.00         0.00           P4         0.00         0.00           P4         0.00         0.00           P5         0.00         0.00           P6         0.00         0.02	P1         0.00         0.00         0.00           P2         0.00         0.00         0.00           P3         0.00         0.00         0.00           P4         0.00         0.00         0.00           P5         0.00         0.00         0.00           P6         0.00         0.28         0.00           P7         0.00         0.28         0.00           P8         0.00         0.28         0.00           P9         0.00         0.00         0.00           P1         -0.05         0.00         0.00           P3         0.00         0.00         0.00           P3         0.00         0.00         0.00           P3         0.00         0.00         0.00           P4         0.00         0.00         0.00           P5         0.00         0.00         0.00           P6         0.00         0.09         0.00           P7         0.00         0.28         0.00	P1         0.00         0.00         0.00         0.00           P2         0.00         0.00         0.00         0.18           P3         0.00         0.00         0.00         0.00           P4         0.00         0.00         0.00         0.00           P5         0.00         0.00         0.00         0.00           P6         0.00         0.28         0.00         0.14           P8         0.00         0.28         0.00         0.28           P9         0.00         0.28         0.00         0.00           P1         -0.05         0.00         0.00         0.00           P2         0.00         0.00         0.00         0.00           P3         0.00         0.00         0.00         0.00           P4         0.00         0.00         0.00         0.00           P3         0.00         0.00         0.00         0.00           P4         0.00         0.00         0.00         0.00           P5         0.00         0.09         0.00         0.14           P7         0.00         0.28         0.00         0.14	P1         0.00         0.00         0.00         0.00         0.00         0.00           P2         0.00         0.00         0.00         0.18         923.88           P3         0.00         0.00         0.00         0.00         707.11           P4         0.00         0.00         0.00         0.00         382.68           P5         0.00         0.00         0.00         0.00         0.00           P6         0.00         0.28         0.00         0.14         0.00           P8         0.00         0.28         0.00         0.28         0.00           P9         0.00         0.00         0.00         0.00         0.00           P1         -0.05         0.00         0.00         0.00         0.00           P2         0.00         0.00         0.00         0.00         0.00           P2         0.00         0.00         0.00         0.00         0.00           P2         0.00         0.00         0.00         0.00         -0.02           P3         0.00         0.00         0.00         0.00         -0.02           P4         0.00         0.00	P1         0.00         0.00         0.00         0.00         0.00         0.00           P2         0.00         0.00         0.00         0.00         0.00         923.88         0.00           P3         0.00         0.00         0.00         0.00         707.11         0.07           P4         0.00         0.00         0.00         0.00         382.68         0.04           P5         0.00         0.00         0.00         0.00         382.68         0.04           P5         0.00         0.00         0.00         0.00         0.00         0.00         0.00           P6         0.00         0.02         0.00         0.14         0.00         0.42           P8         0.00         0.28         0.00         0.28         0.00         0.00         0.00           P1         -0.05         0.00         0.00         0.00         0.00         0.00           P3         0.00         0.00         0.00         0.00         0.00         0.00           P3         0.00         0.00         0.00         0.00         0.00         0.00           P3         0.00         0.00         0.0	P1         0.00         0.00         0.00         1000.00         0.00         0.00           P2         0.00         0.00         0.00         0.18         923.88         0.00         382.68           P3         0.00         0.00         0.00         0.00         707.11         0.07         707.11           P4         0.00         0.00         0.00         0.00         382.68         0.04         923.88           P5         0.00         0.00         0.00         0.00         382.68         0.04         923.88           P5         0.00         0.00         0.00         0.00         0.00         1000.00           P6         0.00         0.00         0.00         0.00         0.00         0.00         923.88           P7         0.00         0.28         0.00         0.14         0.00         0.42         707.11           P8         0.00         0.28         0.00         0.28         0.00         0.26         382.68           P9         0.00         0.00         0.00         0.00         0.00         0.00         0.00           P1         -0.05         0.00         0.00         0.00	P1         0.00         0.00         0.00         100.00         0.00         0.00         0.00           P2         0.00         0.00         0.00         0.18         923.88         0.00         382.68         0.00           P3         0.00         0.00         0.00         0.00         707.11         0.07         707.11         0.14           P4         0.00         0.00         0.00         0.00         382.68         0.04         923.88         0.08           P5         0.00         0.00         0.00         0.00         0.00         0.00         1000.00         0.00           P6         0.00         0.00         0.00         0.00         0.00         0.00         1000.00         0.00           P6         0.00         0.28         0.00         0.14         0.00         0.42         707.11         0.57           P8         0.00         0.28         0.00         0.28         0.00         0.26         382.68         0.50           P9         0.00         0.00         0.00         0.00         0.00         0.00         0.00           P1         -0.5         0.00         0.00         0.00	P1         0.00         0.00         0.00         1000.00         0.00 <t< th=""><th>P1         0.00         0.00         0.00         1000.00         <t< th=""><th>P1         0.00         0</th><th>P1         0.00         0.00         0.00         1000.00         <t< th=""></t<></th></t<></th></t<>	P1         0.00         0.00         0.00         1000.00         0.00 <t< th=""><th>P1         0.00         0</th><th>P1         0.00         0.00         0.00         1000.00         <t< th=""></t<></th></t<>	P1         0.00         0	P1         0.00         0.00         0.00         1000.00         0.00 <t< th=""></t<>



## H10 test – Description (1)

- Ariane IV 3rd stage, standard CADET target
- Analyze target thermal behavior to allow IR tracking
- Test orbital parameters:

Radius <i>r</i>	7161 km
Eccentricity e	0
Inclination <i>i</i>	45°
Argument of periapsis $\omega$	0°
Ascending node $\Omega$	-90°

- Attitude: LOCS, Z body aligned with  $-\vec{V}$ , Y body aimed to Z Earth
- Optical properties: guess, obtained through aerospace materials data base ( $\overline{\alpha}$ =0.537,  $\overline{\varepsilon}$ =0.266)
- Ray density (rays/m<sup>2</sup>): 10k (Sun), 100k (Earth, albedo)
- 41 orbital position computed (half orbit, no eclipse)

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Case	ESATAN TMS	CADET	Case	ESATAN TMS	CADET	Δ X1000	۵%	
# GR	9453	9287	$\sum$ gr	83.070	83.154	84.240	0.101	
Common GR	64	95	$\sum GR_{Model to space}$	48.304	48.298	-6.476	-0.013	
Additional GR	2958 2792		$\sum GR_{Model to inactive}$	6.595	6.595	0.834	0.012	
$\sum {\sf GR}_{{\sf Uncommon}}$	1.2167e-3	57.818e-3	<b>GR</b> <sub>Model to model</sub>	28.17	28.26	89.882	0.319	
Max Gr <sub>Uncommon</sub>	0.1372e-3	1.079e-3		83.068	83.096	27.859	0.033	
			0.31389	0.31152	2.372	0.755		
ESATAN and CADET GR cut off value: 1e-6 28 <sup>th</sup> European Space Thermal Analysis Workshop 14-15 October 2014, ESA/ESTEC Sheet 27								



Pe	Performance – Test Hardware										
				Clock		M	emory		Peak performances		
Device	Vendor	Туре	CU	GHz	Туре	GB	Float4 GB/s	Float16 GB/s	Int4 GIOPS	Float4 GFLOPS	Float16 GFLOPS
Core i7 940	Intel	CPU	4+4	2.93	DDR3	18	12.29	12.29	8.90	27.77	25.69
Core i3 2370M	Intel	CPU	2+2	2.40	DDR3	4	9.56	9.06	/	19.12	19.12
Core i3 3220	Intel	CPU	2+2	3.30	DDR3	8	10.96	11.05	/	26.19	26.61
Core i7 4700HQ	Intel	CPU	2.4	2.40	DDR3	8	17.20	17.09	/	35.06	36.71
GT 630	NVIDIA	GPU	2	1.62	GDDR3	1	17.52	4.56	103.07	307.50	280.09
GTX 670M	NVIDIA	GPU	7	1.20	GDDR5	1.5	61.46	15.36	/	786.62	718.22
GT 750M	NVIDIA	GPU	2	1.10	DDR3	4	25.60	11.64	/	740.01	740.00
GTX Titan Black	NVIDIA	GPU	15	0.98	GDDR5	6	298.26	107.37	1010.58	4685.42	4685.42
Quadro 2000	NVIDIA	GPU	4	1.25	GDDR5	1	35.87	8.97	158.94	472.28	459.16
HD 5850	AMD	GPU	18	0.725	GDDR5	1	86.04	34.41	443.27	1738.85	1782.76
HD 7870 GE	AMD	GPU	20	1.00	GDDR5	2	130.31	35.51	505.76	2507.83	437.86
HD 7950 Boost	AMD	GPU	28	1.15	GDDR5	3	278.37	48.54	748.95	3725.15	3650.85
HD 8970M	AMD	APU*	5	0.825	DDR3	2	7.99	2.21	/	251.56	247.00
* Accelerated Pro- 28 <sup>th</sup> European 14-15 October Sheet 29	AMD APU 5 0.825 DDR3 2 7.99 2.21 / 251.56 247.00 * Accelerated Processing Unit, AMD definition of a chip which contains a CPU section and a GPU section 28 <sup>th</sup> European Space Thermal Analysis Workshop 14-15 October 2014, ESA/ESTEC Sheet 29										+ Ie eering

	Tracing	, Mr/s		Execution times, seconds						
Device	Sun	REF Planet	41 Sun fluxes	Sun, mean	GR + UV REF	41 Earth + Albedo (CPU)	Earth + Albedo, mean	Total	Gain	
Core i7 940	2.25	1.61	57.21	1.40	224.28	8.94	0.22	302.66	3.24	
Core i3 2370M	1.21	0.65	240.72	5.87	590.10	15.02	0.40	863.11	1.14	
Core i3 3220	1.23	1.01	106.41	2.60	378.89	20.14	0.50	524.39	1.87	
Core i7 4700HQ	2.25	1.56	57.14	1.39	231.73	5.17	0.13	303.27	3.24	
GT 630	2.02	1.33	62.98	1.54	307.10	20.15	0.48	410.16	2.39	
GTX 670M	4.29	3.39	29.61	0.72	119.21	12.70	0.31	167.00	5.88	
GT 750M	2.73	1.99	46.61	1.14	158.05	5.53	0.19	218.61	4.49	
GTX Titan Black	9.42	13.35	13.49	0.33	30.24	7.12	0.17	53.84	18.23	
Quadro 2000	1.65	1.29	40.82	1.00	302.21	7.68	0.19	357.95	2.74	
HD 5850	3.61	4.34	35.26	0.86	94.15	5.13	0.19	144.74	6.78	
HD 7870 GE	6.21	8.52	20.71	0.51	47.60	5.07	0.12	81.58	12.03	
HD 7950 Boost	8.18	13.85	15.54	0.38	29.48	6.03	0.15	58.93	16.66	
HD 8970M	3.08	2.85	41.23	1.01	143.36	5.16	0.14	197.28	4.98	
ESATAN TMS <sup>*</sup>	/	/	319.00	7.78	650.00	12.50	0.30	981.50	1.00	
* Calculation All computat 28 <sup>th</sup> European S 14-15 October 2	on Intel tions on V Space The 2014, ESA	i7 940 2.9 Vindows ermal Ana /ESTEC	93 GHz; sii 7/8 64 ma Iysis Worl	ngle core ichines; to kshop	executior ools also v	n with Intel Turbo vorks on Linux	Boost, (clock set	to 3.2 G⊦ ★ ★	Iz)	











### **Possible Improvements**

- Data flow:
  - Float16 to float4 data items conversion
  - Data caching through constant memory blocks for initialization (BVH data etc.)
  - Data caching through texture units (simpler if OpenCL 1.2 is used)
- Improve BVH structure (Split BVH construction  $\rightarrow$  SBVH)
- Stack-less tracing kernel (reduce register pressure and improve the number of concurrent threads)
- Take advantage of multiple devices (multi GPU, GPU+CPU configurations)
- Evaluate different ray tracing strategies:
  - Offloading part of the ray tracing procedure to the CPU when few rays need to be traced, and leave on device only mass evaluations
  - Use device fission (OpenCL 1.2) to parallelize ray spawning and ray tracing on device, in order to maximize device occupancy



## Conclusions

- CADET radiative solver is implemented and its results are consistent with the ESATAN TMS tool (considering RTMC fluctuations).
- On GPU devices, the tool use the huge computation power of GPU HW and get acceptable performances (up to 18x respect to ESATAN TMS on high end hardware).
- Additional speedup of 10x and more could be achieved improving the tool (compared to NVIDIA computer graphics rendering algorithm).
- New developers' skills are needed to maximize GPGPU performances.

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