

Appendix I

Thermal model correlation using Genetic Algorithms

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THERMAL MODEL CORRELATION USING GENETIC ALGORITHMS

21st European Workshop on Thermal and ECLS Software

ESTEC, 30-31 Octobre 2007

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All the space you need



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All the space you need
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Thermal Model Correlation Using Genetic Algorithms
21st Thermal & ECLS Workshop-ESTEC



Study context

- ESA contract number: 19840/06/NL/PA
- **Goal:** Evaluate feasibility of using **Genetic Algorithms (GAs)** to address the general issue of **post- test thermal model correlation**.
- Thermal model correlation = An optimization problem
Reduce difference between model predictions and test measurements
- Thermal background: problem is complex:
⇒ *Collaboration with optimization specialized researchers to find/perfect a method appropriate to our problem.*

Nicolas DURAND: DSNA/DTI/R&D/POM (ENAC Toulouse)
Use of GAs to solve Air Traffic Control problems

Description of Thermal model correlation problem

A complex problem...

- Many variables to be simultaneously correlated
- Function shape is very hilly ⇒ Many different local minimums
- No analytical expression of the function.

Use of a global method to explore the whole domain and identify the global solution.

- Deterministic methods: Restricted to reduced number of parameters and specific problems.
- Stochastic methods (GAs, etc): Results depend from previous data computed but also random seeds. Suitable to many problems

Note: Thermal model correlation process specificity:

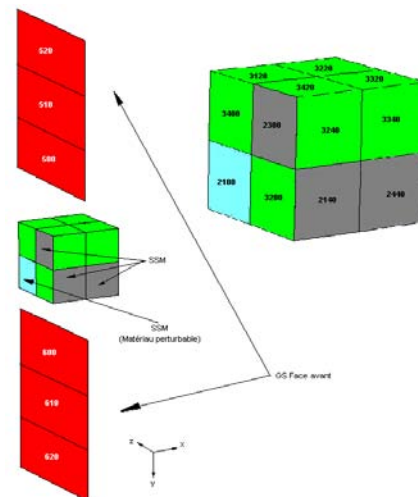
Fitness function computation cost very high compared to usual optimization problems

Chosen approach: Method testing rationale

- Use of a **“theoretical” numerical based only approach**
 - Models are perturbed by changing parameter values.
 - ‘Test measurements’ temperatures used for correlation correspond to model predictions, before introducing perturbation.
- **Simultaneous** correlation for two test cases (hot + cold), steady-state conditions only.
- Test Cases definition
 - Tested on small size TMM models only (up to 280 Nodes)
 - Test first the method for a reduced number of correlation parameters (5).
 - Then extend it to a larger number of parameters representative of future industrial problems (up to 20 parameters).

Tested models

- Model1: Studybook case model
 - 100 nodes, usual modelling situations (dissip. unit in enclosure+ radiator, MLI, structural panels , solar array)
 - 21 TMM parameters:
 - Dissipation and conductive aspects (λ longi & transverse, thickness, Contact and MLI efficiency.
 - 2 measurement point sets \Rightarrow *Evaluate impact of instrumentation*
 - Model 2: instrument phase B model
 - 280 nodes, 17 TMM parameters (dissipation & conductive aspects).
- Note:** Model computation speed increased by directly running executable file (correlation parameters values read from input file)

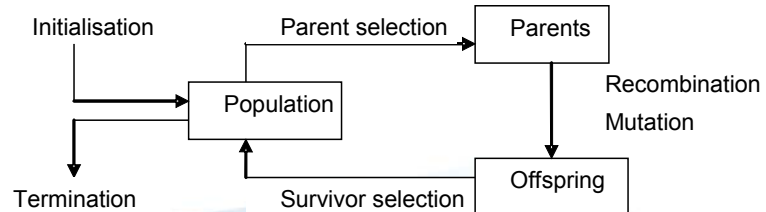


Basics about Genetic Algorithms (1/3)

- Optimization method based on Darwin evolution's theory
 " Within a given population, only the most suited individuals survive and have offspring "
 ⇒ *The specie improves with elapsed time.*
- Transposition to numerical world

Life	Mathematics	<i>TMM correlation</i>
Chromosome	function parameter	<i>TMM parameter</i>
Adaptation criterion	function result	ΔT (Test measurement, TMM prediction)

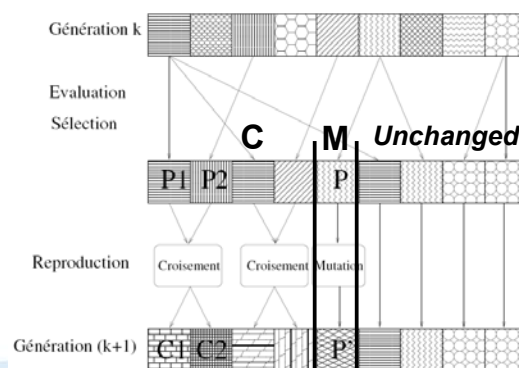
- How does it work in practice ?



Basics about Genetic Algorithms (2/3)

Remarks

- Operators
 - Variation operators: Allow to explore the domain (close or far from current solution).
 - Mutation is common to all stochastic methods.
 - Crossover is specific to Genetic Algorithms: exploit parents properties to propose a new solution
 - Selection operator: allows to converge to the best solution.



Basics about Genetic Algorithms (3/3)

Remarks (end)

- Good GA operation = Balance between domain exploration and fast convergence
- GA Implementation
 - Many possible technical solutions for the elementary bricks
 - Many associated GA parameters may be tuned to get a better behaviour

GA kernel good programming is a matter of experience

GA optimization itself is problem specific and also a matter of experience

Practical applicability of GA to thermal model correlation

- **Any change in correlation problem definition generate a new optimization problem**
 - TMM used
 - Modelling change in TMM
 - Correlation parameters used
 - Measurement points used

- **Thermal engineers are not optimization / GA specialists**

Questions to be answered by the study:

- Does GA allow to find the solution to the thermal problem ?
- Is there a given (\approx frozen) simple GA parameterization globally suitable to thermal correlation problem ?

\Rightarrow To be evaluated in this study for two small models only

Test plan definition (1/3)

- Evaluate which value(s) of three most important GA parameters should be suited to thermal problem :
 - Population size
 - Crossover rate
 - Mutation

- Evaluate robustness of GA to different thermal model problems
 - Change of TMM
 - Change of correlation parameter set used
 - Change of measurement point set used

Test plan definition (2/3)

For each model

- 4 to 5 different values of population size
values defined based on number of correlation parameters used
- 10 different (Crossover rate x Mutation rate) configurations

	Crossover rate			
Mutation rate	0	0,2	0,4	0,6
0,2	x	x	x	x
0,4	x	x	x	
0,6	x	x		
0,8	x			

- Tested TMM correlation parameter configurations
 - 8 different reduced configurations (5 parameters)
 - 1 large configuration (~ 20 parameters)
- Two different measurement point sets
- For a given test case, 4 to 5 different runs with different random seeds

Test plan definition (3/3)

Stop criterion

- Fitness function definition

$$FF = \sum_{thcases} \sum_{measnodes} (T_{pred} - T_{meas})^2$$

Note: Standardized measurement of model discrepancy

Average Model Correlation Accuracy (AMCA) in °C:

$$AMCA = \sqrt{\frac{\sum_{thcases} \sum_{measnodes} (T_{pred} - T_{meas})^2}{nbcases.nbmeasnodes}}$$

- Success definition
 - $FF < 0.01 \Rightarrow$ Max discrepancy on any point $< 0.1^\circ\text{C}$
 - Max nb of computed generations = 500

Tests results : Sensitivity to population size

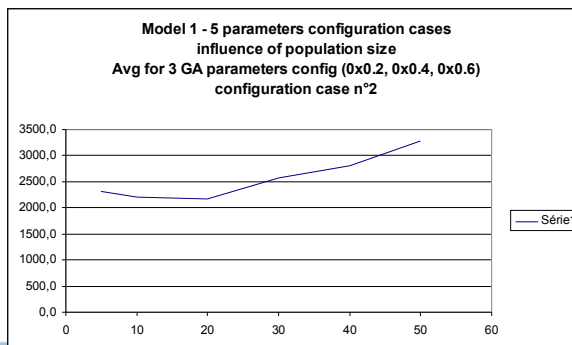
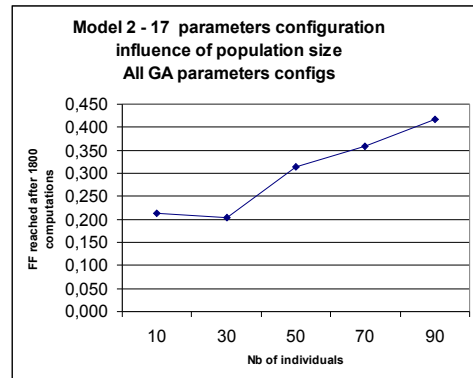
better results with small values

Optimum seems to be between

nb correl. parameter &

2 x nb.correl. parameter

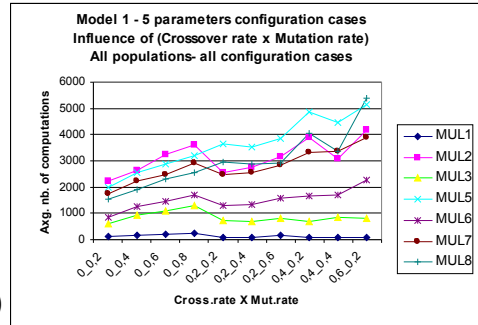
Note: Never go lower than 10 to still have a GA.



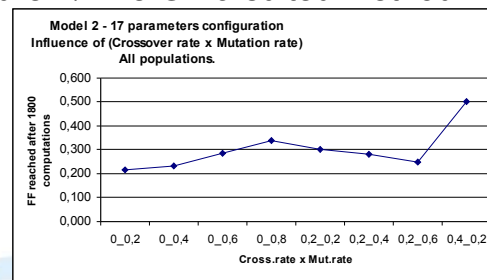
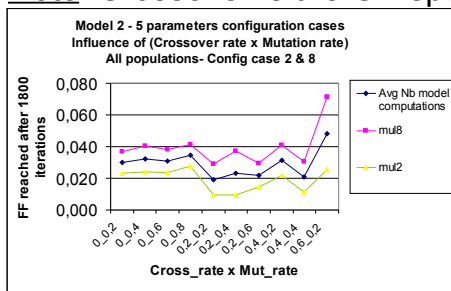
\Rightarrow Are GA a suited method ?

Tests results : Crossover rate x Mutation rate

- Easy situations
 - No crossover needed
 - Mutation should be low (0.2)
- Difficult situations
 - A bit of crossover may be used (0.2)
 - Mutation should be kept low



Note: Crossover is the GA specific feature ⇒ Are GA a suited method ?



Tests results: Influence of parameter set used for correlation

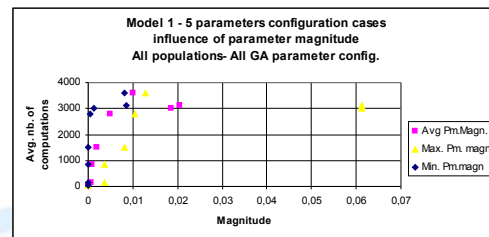
- Simulation duration increases with number of involved parameters.

Test cases	Avg nb.Comp.
5 param.config. Population: 20 to 40 individuals Easy configuration	843
Hard configuration	3208
21 param.config Population: 60 to 100 individuals	33072

- GA operation depends on parameter configuration
- Simulation duration increases with magnitude of parameters.

Magnitude= Potential impact of parameter on FF value when varying in its allowed domain.

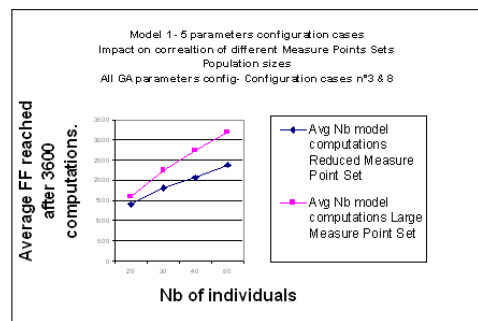
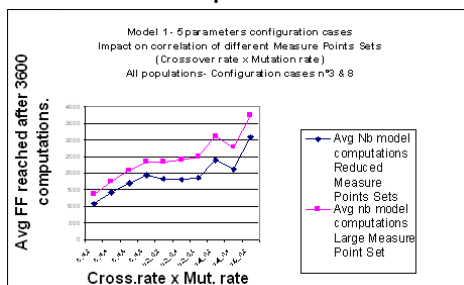
Note: Only main magnitude params. are initially taken into account by the optimization process
⇒ *Incremental correlation approach?*



Tests results : Influence of Measurement set used.

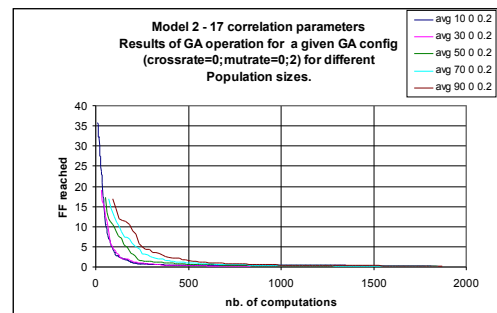
- Tested on model1
 - 1st Measurement set used (standard): 22 points
 - 2nd Measurement set used: 35 points
- FF success criterion trimmed to get comparable results.*
- Similar results obtained for 2ns measurement point sets.
 - Model more difficult to correlate: More constraints to be solved

Due to more points involved ?



Tests results : Convergence speed

- GA has a fast initial convergence (to find areas where are solutions) but a slow finishing
- ⇒ No interest of insisting with GA operation



Note: Results obtained with GA are already interesting.

Example

Model 1 – 21 parameters

AMCA $\approx 0.1^\circ\text{C}$ after 1000 computations

But problem (model, nb of measure points) remains simple

Tests results :

Comparison with random search

Fitness obtained for a given number of model computations =
4000 in random search

Tested for 5 parameters configuration from model 1

	GA results		Random search	
	nb. Runs	end FF	Nb runs	end FF
MUL2	2471	0,01	4000	0,1
MUL8	1991	0,01	4000	0,56

GA is much better than a random search !

Conclusion (1/3)

- GA allows to identify areas where the best correlation solution is ... but not to converge finely on it.
 - This convergence may be sufficient.

The whole allowed domain has been explored

→ *The order of magnitude of correlation reachable with this model has been found.*

⇒ For additional correlation improvement, need to change model:

 - Correlation parameter choice
 - Variation domain for parameters
 - TMM modelling
- Capacity to correlate several cases in one shot (fitness function definition)

Conclusion (2/3)

- GA parameterization:
Some simple preliminary guide lines for thermal model correlation may be proposed
(*TBC, for DSNA/POM GA implementation only*)

- Computation cost is a key issue.

Estimated –minimum-: Run of 500 to 1000 cases for just one correlation simulation.

⇒Needs to drastically increase computation power available to address industrial cases: (large model, transient conditions).

Clusters + parallelization ...

⇒Optimization process to be improved:

- Evaluation of alternative global methods.
- Couple local method to initial global method step.

Conclusion (3/3)

GAs Evaluated on 2 small models only

Results need to be confirmed by much more tests on different models.

- Thermal model correlation is a complex problem requiring complementary skills:
Thermal engineering/ Numerical optimization/ Software engineering
- Fruitful collaboration achieved with DSNA/DTI/R&D/POM team have allowed to really progress on the matter

Great thanks to Nicolas DURAND for its 1st class support all along this project !

