

## Modelling of Cryocoolers

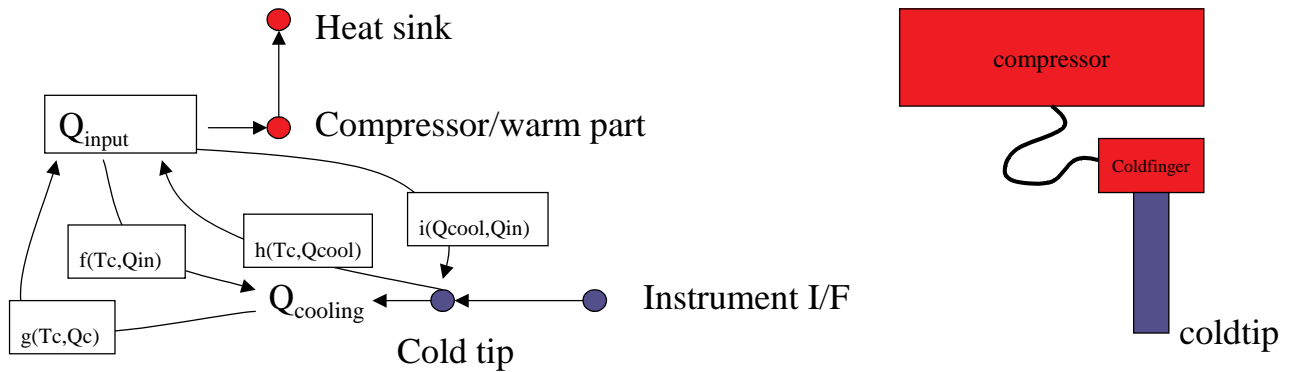
## Introduction

- *Current cryocooler models in ESATAN make use of polynomial fit functions in combination with boundary nodes*
- *This limits the number of free parameters (e.g. heat sink temperature)*

*therefore*

- *Leading to a conservative design only considering worst cases*
- *It is difficult to perform sensitivities or assess the impact of sub-systems (e.g. compressor performances)*
- *A correct heat balance is not always obtained*

## Stirling/ Pulse Tube models



$$Q_{input} = a Q_{cool}^2 + b Q_{cool} + c$$

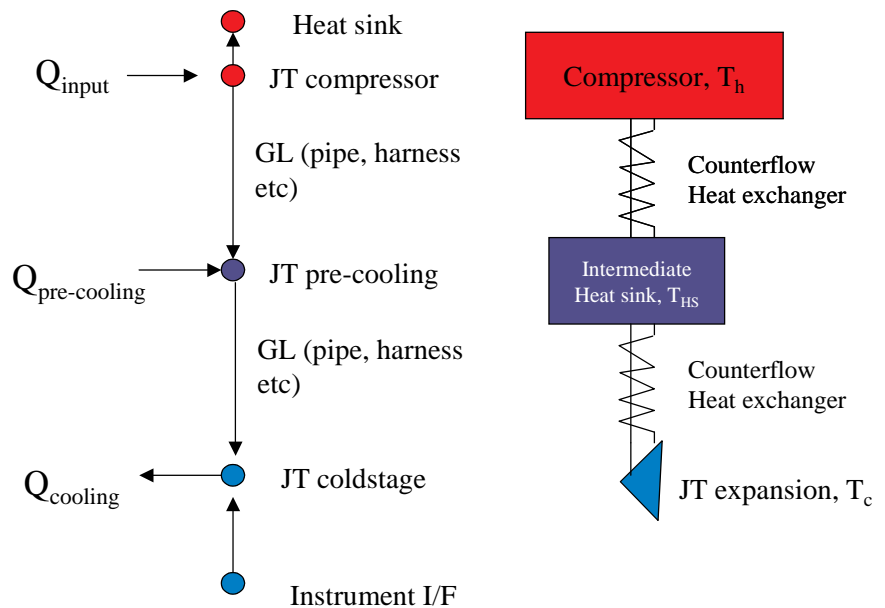
$$h(T_c, Q_{cool}): \quad a = a_1 T_{cold\ tip}^2 + a_2 T_{cold\ tip} + a_3$$

$$b = b_1 T_{cold\ tip}^2 + b_2 T_{cold\ tip} + b_3$$

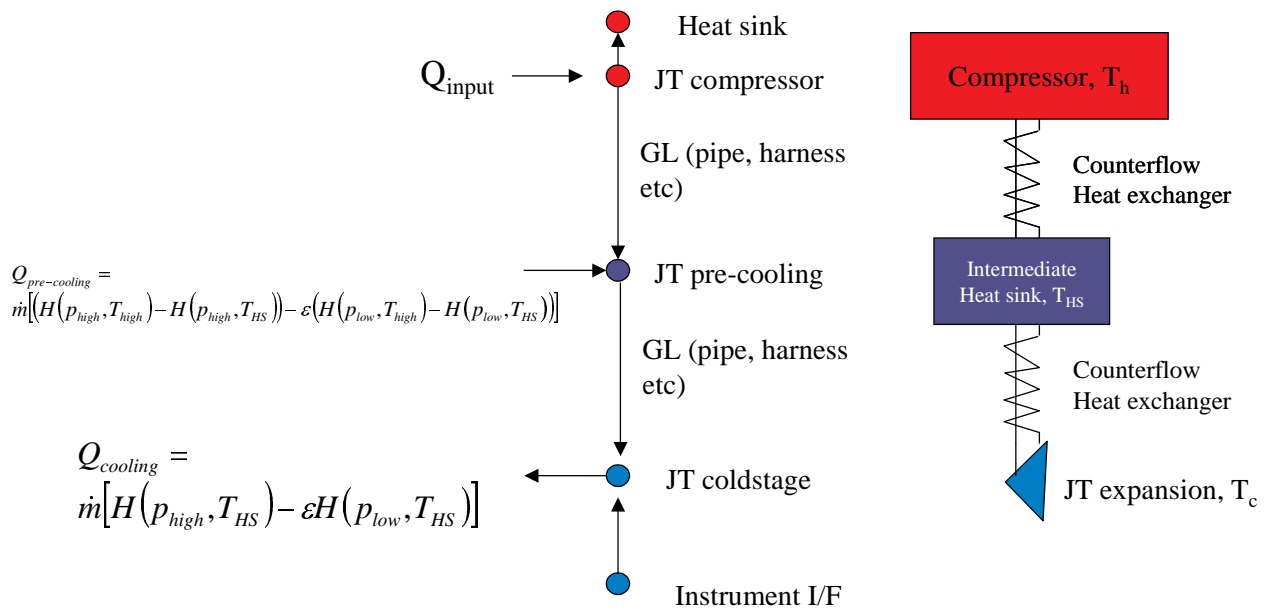
$$c = c_1 T_{cold\ tip}^2 + c_2 T_{cold\ tip} + c_3$$

## Joule Thomson coolers

$Q_{pre-cooling}$  and  $Q_{cooling}$ , depending on the Hx efficiency and the fluid, are provided only by polynomial fits



## Joule Thomson coolers including Physics



## Requirements for Cooler models

- In most cases the coldtip temperature is specified by the system (coming from detector needs etc)
- The required cooling power is obtained by the TMM
- For sizing the thermal system the cooler model must provide

$$Q_{input} = f(T_{coldtip}, Q_{cooling})$$

- For transient verification, the cooler model must be able to calculate  $T_{cold}$  for a given  $Q_{input}$ . The following function is required within a TMM:

$$Q_{cooling} = g(T_{coldtip}, Q_{input})$$

## Requirements for Cooler models

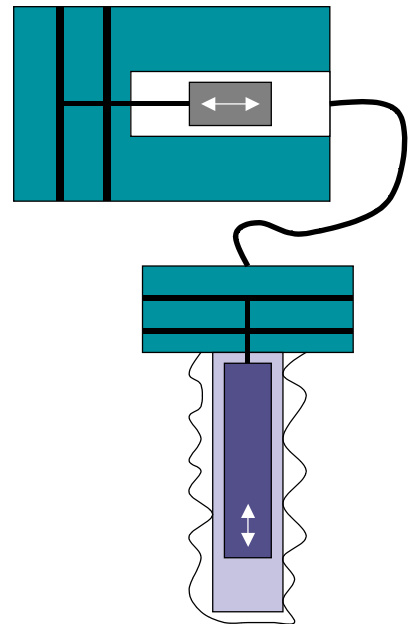
- Cooler model shall consider as a minimum the following parameters:
  - For single stage cooler  $T_{\text{heat sink}}, T_{\text{coldtip}}, Q_{\text{input}}, Q_{\text{cooling}}$
  - For multistage coolers, the influence of the intermediate cooling stages for different operating conditions needs to be implemented
- This can not be handled by polynomial fits or would require a large amount of data points at specific conditions (e.g. isothermal points)

## Requirements for Cooler models

- Overall heat balance needs to be correct
  - Common approach is:  $Q_{\text{dissipated}} = Q_{\text{input}}$
  - For Stirling, PT and reverse Turbo-Brayton correct approach is:  $Q_{\text{dissipated}} = Q_{\text{input}} + Q_{\text{cooling}}$
- Use of boundary nodes shall be limited, where required link them correctly with the TMM
- Shall be simple, fast and robust

## Stirling cooler

- Compressor transform electrical Energy into pneumatic Work ( $pV$  work). For high efficient space coolers one can assume:  
 $pV = Q_{in} - \dot{p}R$
- Pressure wave generated passes through a regenerative heat exchanger (= Regenerator)
- At the cold end the pressure wave and massflow wave are shifted such, that the following cooling occurs:  
 $q_{gross} = T_{cold} / (T_{hot} - T_{cold}) * pV$
- The available cooling power is:  
 $q_{net} = q_{gross} - losses$
- Main losses are:  
conductive, radiative, regenerator and shuttle losses



## Stirling cooler losses

- Conductive/radiative losses are equal to parasitic loads of a non-operating cooler.
- Regenerator losses:  
 $Q_{regenerator} = dm/dt * c_p * (T_{hot} - T_{cold}) (1 - \epsilon)$   
with  $dm/dt \sim pV/T_{hot}$
- Shuttle losses  $Q_{shuttle} \sim (T_{hot} - T_{cold})/stroke$

## Stirling cooler equation

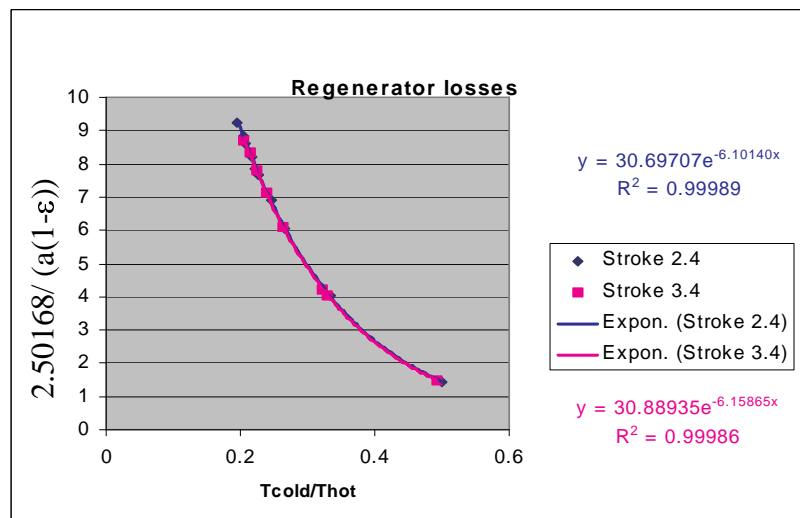
- It should be possible to describe the Stirling cooler with the following equation:

$$\frac{T_{cold}}{T_{hot} - T_{cold}} pV - c(T_{hot} - T_{cold}) - a(1 - \epsilon_{reg}) \frac{pV}{T_{hot}} (T_{hot} - T_{cold}) - b \frac{T_{hot} - T_{cold}}{\text{stroke}} - q_{net} = 0$$

- Approach has been tested with MIPAS 50-80k Astrium cooler data, assuming a constant compressor efficiency (due to the lack of PR data)

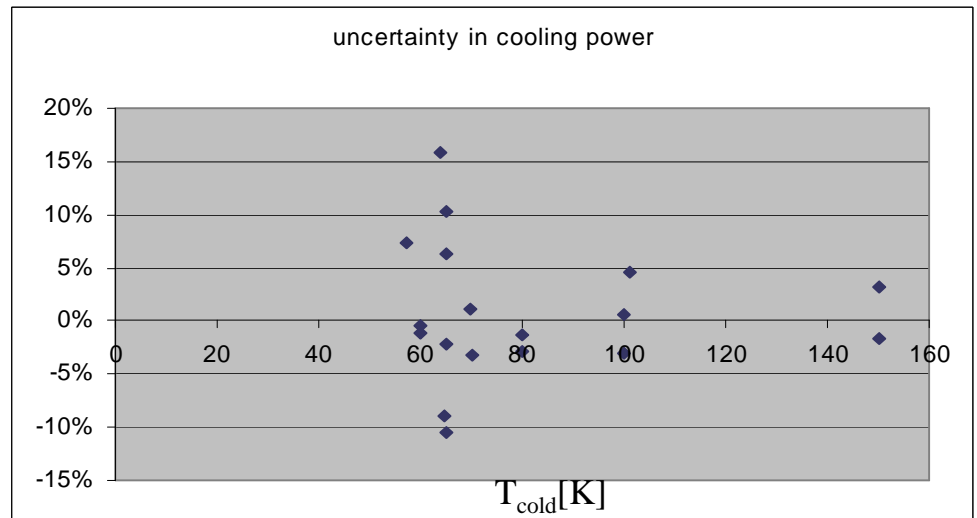
## Stirling cooler extrapolation

- Dataset includes 18 measurements from 57-150K and -10°C to 40°C heat sink
- $pV = 0.8 * Q_{in}$
- $C = 220 \text{ mW} / 193\text{K}$  from parasitic measurements, refined during interpolation
- Distinguishing between regenerator and shuttle loss not possible, but regenerator loss as a function of displacer stroke

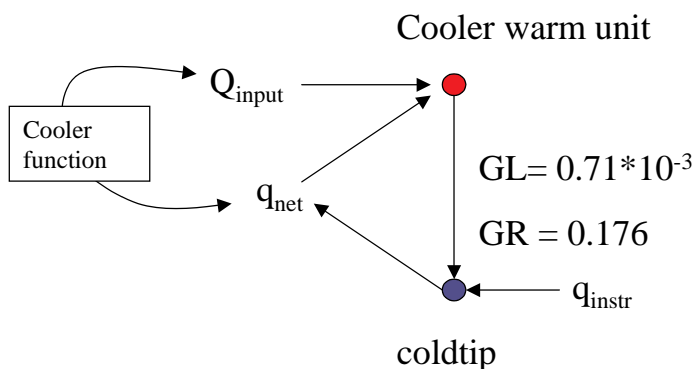


## Stirling cooler extrapolation uncertainty

Strong deviations from measurements above 150K, additional correction for these temperatures required



## Stirling cooler model



Result TMM:

(300mW  $q_{instr}$ , Cooler Wu 263K)

$T_{cold} = 64.9K \rightarrow 12.19W$  input

$Q_{in} = 11.17W \rightarrow 66.1K T_c$

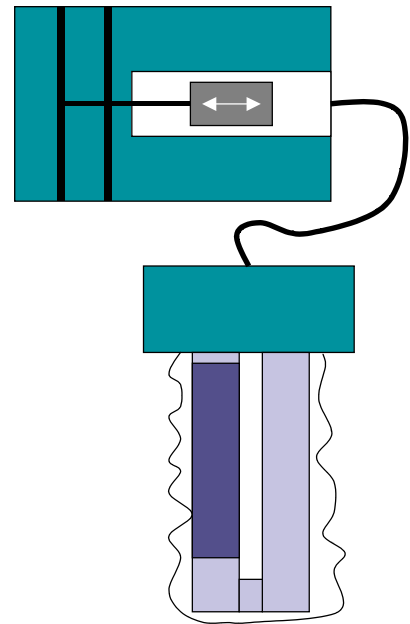
Cooler function:

$$0.8 * Q_{input} \left[ \frac{T_{cold}}{T_{hot} - T_{cold}} - \frac{2.50168}{30.697} e^{6.101 T_{cold}/T_{hot}} \frac{1}{T_{hot}} (T_{hot} - T_{cold}) \right] - q_{net} = 0$$

Note: not valid for temperatures below 50K and above 150K

## Pulse Tube cooler

- Compressor transform electrical Energy into pneumatic Work ( $pV$  work). For high efficient space coolers one can assume:  
 $pV = Q_{in} - \dot{p}R$
- Pressure wave generated passes through a regenerative heat exchanger (= Regenerator)
- At the cold end the pressure wave and massflow wave are shifted such, that the following cooling occurs:  
 $q_{gross} = T_{cold}/T_{hot} * pV$
- The available cooling power is:  
 $q_{net} = q_{gross} - losses$
- Main losses are:  
conductive, radiative, regenerator and pressure losses



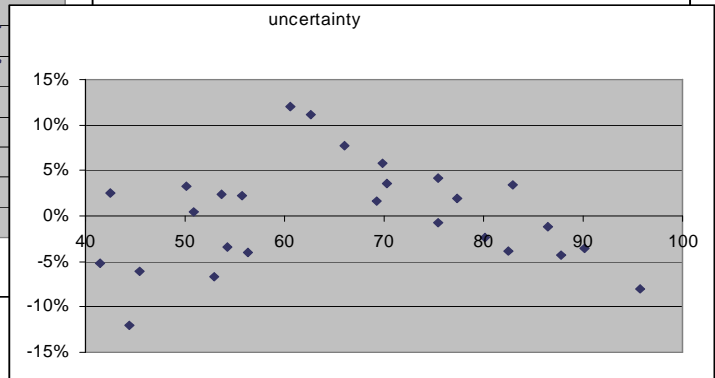
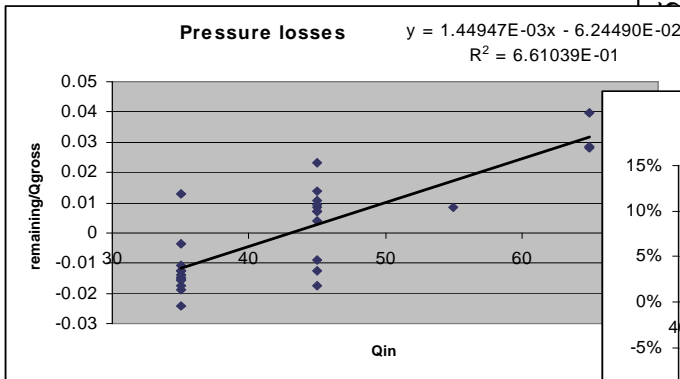
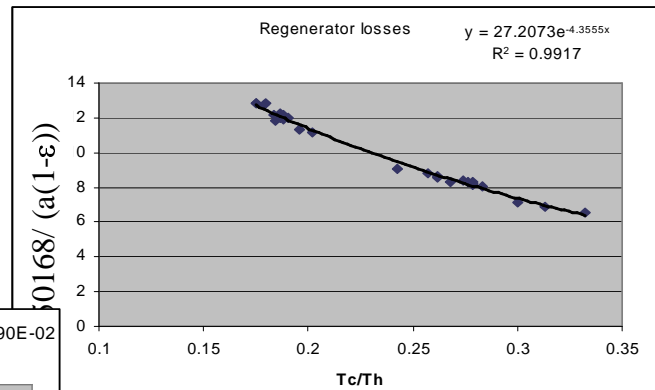
## Pulse Tube cooler losses

- Conductive/radiative losses are equal to parasitic loads of a non-operating cooler.
- Regenerator losses:  
 $Q_{regenerator} = dm/dt * c_p * (T_{hot} - T_{cold}) (1 - \epsilon)$   
with  $dm/dt \sim pV/T_{hot}$
- Pressure losses  $Q_{press} \sim f(p_{ampl}) * T_c/T_h * pV$   
 $p_{ampl} \sim Q_{in}$
- Data taken from MPTC Air liquide TRP cooler



## Pulse Tube cooler extrapolation

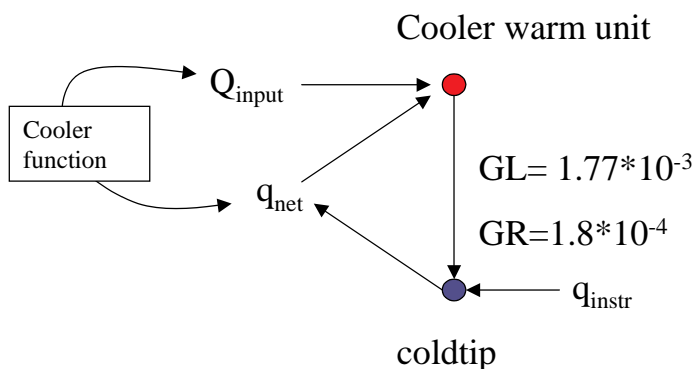
- Dataset includes 23 measurements from 40-95K and -40°C to 40°C heat sink
- $pV = 0.7 * Q_{in}$
- $C = 465 \text{ mW} / 208\text{K}$  from parasitic measurements



5<sup>th</sup> October 2004

Martin Linder

## Pulse Tube cooler model



Result TMM:

$$T_{cold} = 60.63\text{K}, T_{hot} = 310\text{K}, q_{instr} = 0$$

$$Q_{in} = 45\text{W} \rightarrow 58.7 \text{ K } T_c$$

$$T_{cold} = 75.43\text{K}, T_{hot} = 273\text{K}, q_{instr} = 1\text{W} \rightarrow 36.3 \text{ W}$$

$$Q_{in} = 35\text{W} \rightarrow 76.3 \text{ K } T_c$$

Cooler function:

$$0.7 * Q_{input} \left[ \frac{T_{cold}}{T_{hot}} \left( 1.0637 - 1.479 * 10^{-3} * Q_{input} \right) - \frac{2.50168}{27.1518} e^{4.327 \frac{T_{cold}}{T_{hot}}} \frac{(T_{hot} - T_{cold})}{T_{hot}} \right] - q_{net} = 0$$

Note: function not valid for input powers below 30W and  $T_{coldtip}$  above 100K, not verified for high  $T_{coldtip}$

5<sup>th</sup> October 2004

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## Conclusion

- *Performance predictions of Stirling and PT coolers is feasible by interpolating the various loss mechanisms, requiring much less input data than polynomial fits*
- *Some additional effort is required for high cold tip temperatures, mainly for cool down predictions*
- *In addition to the classical thermal parameters, the compressor efficiency also needs to be measured*

## Future work

- *Distinguish between Compressor and warm part of coldfinger and predict dissipated power on each*
- *Modelling of the gas temperature as a function of gross cooling power and I/F temperature (to improve high temperature performance)*
- *Extend model to multistage Stirling and Pulse Tube cooler*