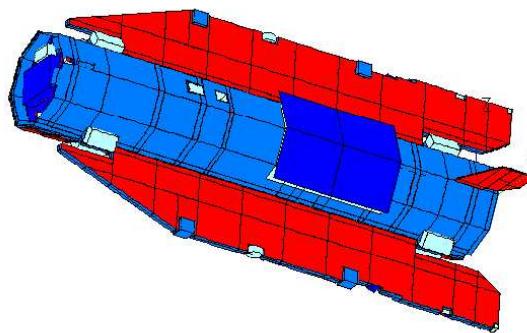


# GOCE

## Thermo-Elastic Distortion Analysis

22.10.2003



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Seite 1

## GOCE - Thermo-Elastic Distortion Analysis

### Content

- GOCE Mission
- Analysis Approach
- Mechanical and Thermal Model and Analysis
- Results
- Summary

Seite 2

## GOCE - Thermo-Elastic Distortion Analysis

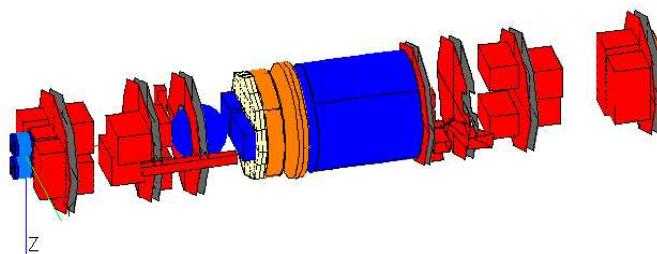
### GOCE Mission - Objectives



- Provide global and regional models of the earth's gravity field with high spatial resolution and high accuracy

Measurement Techniques used:

- Satellite gravity gradiometry - SGG - technique (gravity gradient tensor by Gradiometer (EGG))
- Orbit determination by satellite-to-satellite tracking (SST) with GPS and GLONASS and
- Laser Ranging



Seite 3

## GOCE - Thermo-Elastic Distortion Analysis

### GOCE Mission - Requirements

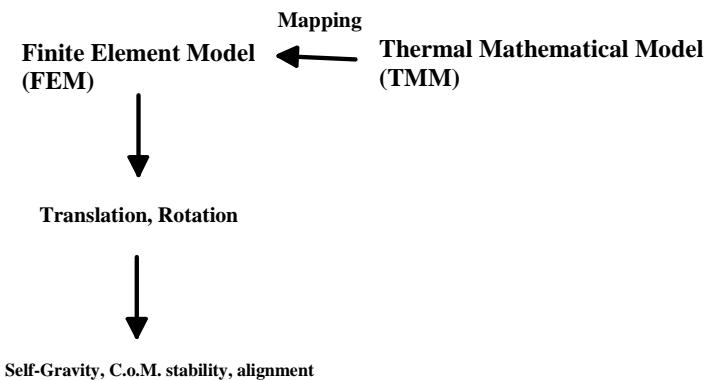


- Stringent requirements for GOCE Platform induced thermal distortions in time and frequency domain cover:
  - Self-gravity acceleration
  - C.o.M. stability
  - Instrument alignment
- MBW: 0.005 Hz to 0.1 Hz
- Thermo-Elastic Distortion Analysis to demonstrate that the requirements are not violated for all measurement phases (incorporates detailed thermal and structure analysis)
- Main distortion sources: time-dependent external heat loads (orbit height = 240-270 km) and internal dissipation of units and thrusters

Seite 4

## GOCE - Thermo-Elastic Distortion Analysis

### Analysis Approach - Common Approach

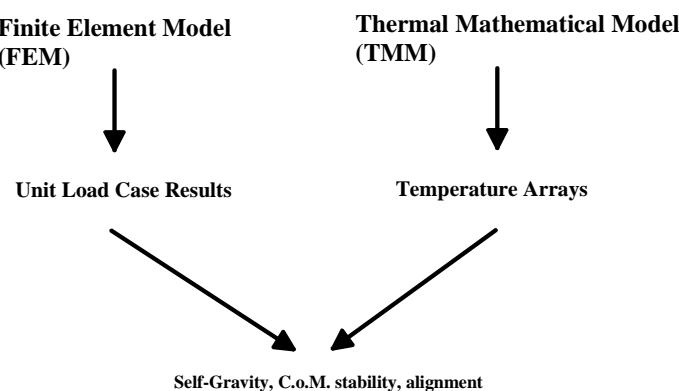


- Time for load case runs and re-runs
- Amount of output data/postprocessing
- Amount of data exchange between TMM and FEM (mapping)

Seite 5

## GOCE - Thermo-Elastic Distortion Analysis

### Analysis Approach – GOCE PFM Approach



- + reduced amount of output data → rapid identification of main distortion sources and design improvements
- + reduced computation time, quick re-analysis, variations and sensitivity analyses possible
- + re-analysis without new FEM analysis
  - o linearization error for self-gravity computations small

Seite 6

## GOCE - Thermo-Elastic Distortion Analysis

### Analysis Approach – GOCE PFM Approach

#### FEM (MSC/Nastran):

- GOCE platform divided into 88 thermal areas
- The thermal areas define the unit load cases
- Starting from a temperature of 20°C for the whole S/C, the temperature of all FE Model nodes of one thermal area is increased by 1°C (remaining FE Model nodes still at 20°C)
- All the required instrument alignment, C.o.M. and self gravity data is calculated per unit load case
- This step is repeated for all unit load cases (thermal areas)

Seite 7

## GOCE - Thermo-Elastic Distortion Analysis

### Analysis Approach – GOCE PFM Approach

#### TMM (ESATAN V 8.7, ESARAD V4.2):

- Computation of transient temperatures for the 88 thermal areas for all time steps
- All temperatures with respect to 20°C (undisturbed)

#### Computation of total distortions for each time step

#### (MS Excel, Mathematica V4.2):

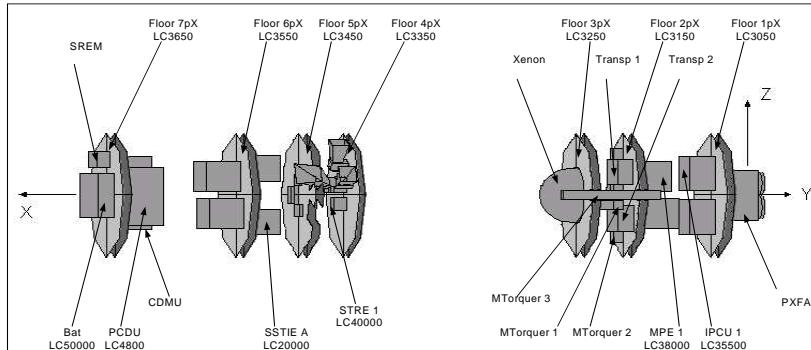
- Multiplication of unit load case results and temperatures (super positioning) → results in time domain
- Fourier transformation afterwards → results in frequency domain (power spectral density - PSD)

Seite 8

# GOCE - Thermo-Elastic Distortion Analysis

## Mechanical and Thermal Model and Analysis

The unit load case results are multiplied with the in-orbit temperatures, calculated with the TMM by using the principle of superposition



Seite 9

# GOCE - Thermo-Elastic Distortion Analysis

## Mechanical and Thermal Model and Analysis

			1	2	3	4
			900	940	1000	1006
Unit load case count						
Unit load case no.						
Unit load case description						
		Basic	Launcher I/F Ring	Launcher I/F Ring	S/C Lateral Panel +Z, -Y	S/C Lateral Panel +Z, -Y
1	GASRF - SSARF 1	phi-xi [rad]	0.20450179579E-09	-1.4789500570E-09	1.3813728904E-08	1.2941527920E-08
		phi-yi [rad]	0.14723187052E-09	-1.0000000000E-09	8.1000000000E-09	8.1000000000E-09
		phi-zi [rad]	0.12054811442E-10	-1.8050144235E-10	8.4465608550E-10	8.7824770000E-10
2	GASRF - SSARF 2	phi-xi [rad]	0.18891985241E-09	-1.3824049495E-09	1.3442162335E-08	1.2137558333E-08
		phi-yi [rad]	0.14673246385E-09	-1.1424602507E-09	8.8058155940E-09	8.1885897183E-08
		phi-zi [rad]	0.12595803233E-10	-4.8156313810E-10	8.4686557230E-09	5.8533052100E-09
3	GASRF - SSARF 3	phi-xi [rad]	0.10728686226E-10	-4.0104084828E-09	4.16104224230E-08	3.7301958652E-08
		phi-yi [rad]	0.91220388973E-10	-4.8020973414E-10	1.1629826302E-08	2.9276602748E-08
		phi-zi [rad]	0.3264607395E-10	1.045318763E-09	3.0290053447E-08	2.8117901591E-08
4	GASRF - SARF	phi-xi [rad]	0.25743256470E-09	4.2141359027E-09	2.5694985725E-09	9.6568637678E-09
		phi-yi [rad]	0.27638708409E-08	-2.5737705421E-08	1.7840012717E-08	1.6895566178E-07
		phi-zi [rad]	0.35159165959E-08	3.8763968453E-08	3.7684338597E-07	-2.0677174323E-07
5	GASRF - GRF	phi-xi [rad]	0.123016000788E-10	1.9295383606E-10	8.1044716273E-09	9.3657207478E-09
		phi-yi [rad]	0.18605552858E-10	-2.0212131273E-10	8.2218160973E-09	1.0953080066E-08
		phi-zi [rad]	0.954698844183E-10	3.9078172623E-09	2.422081155E-09	1.4981697968E-08
6	GASRF - GARF	phi-xi [rad]	0.13090000000E-09	5.0300000000E-09	4.0458439250E-09	1.4130000000E-09
		phi-yi [rad]	0.22232738330E-07	6.1449512606E-08	4.2068688315E-07	1.8667657530E-07
		phi-zi [rad]	0.37238262550E-07	-6.2610583121E-07	1.9506284211E-06	3.4432586857E-07
7	GASRF - MTA -X-Y-Z	phi-xi [rad]	0.3152642739E-07	6.5288479329E-07	3.2545831229E-08	3.3663528150E-08
		phi-yi [rad]	0.28256988549E-07	-8.9304318431E-07	3.0277259350E-07	3.4830347988E-07
		phi-zi [rad]	0.14778127199E-06	6.3302677666E-07	1.0148420464E-08	7.4979953208E-08
8	GASRF - MTA +X+Y+Z	phi-xi [rad]	0.479380448305E-10	3.8415715892E-10	3.7384855428E-09	
		phi-yi [rad]	0.85557400299E-10	-1.1065694081E-09	1.1170631120E-09	4.9037693967E-08
		phi-zi [rad]	0.33377565687E-10	1.389853150E-10	4.5893007650E-09	2.5161050589E-08
9	GASRF - ITA +Z	phi-xi [rad]	0.36065490868E-09	5.8197352369E-09	-9.4749155112E-09	-4.9036693799E-08
		phi-yi [rad]	0.17653220094E-07	4.9014537657E-07	2.9300505252E-07	4.0962574000E-07
		phi-zi [rad]	0.10000000000E-07	4.8999999999E-08	2.9999999999E-07	4.0962574000E-07
10	GASRF - GPS -X	phi-xi [rad]	0.142133477151E-08	-1.4017119565E-08	6.1701141382E-09	-1.3388994868E-08
		phi-yi [rad]	0.24358975233E-10	-1.8357473823E-08	2.8764546377E-08	1.3532339641E-07
		phi-zi [rad]	0.338344239625E-08	3.85028987676E-08	2.8500048200E-08	7.1825415137E-08
11	GASRF - GPS +X	phi-xi [rad]	0.90694493747E-09	-8.9626237867E-09	3.6628238642E-09	-3.9634244998E-09
		phi-yi [rad]	0.15465026525E-09	-3.3030934658E-09	4.2241795371E-08	1.4769733180E-07
		phi-zi [rad]	0.49872752134E-08	-4.9860463895E-08	2.2761015047E-08	6.357382417E-08

Alignment Data computed with FEM (Basic Case and Unit Load Case 1-4 shown)

Seite 10

## GOCE - Thermo-Elastic Distortion Analysis

### Mechanical and Thermal Model and Analysis

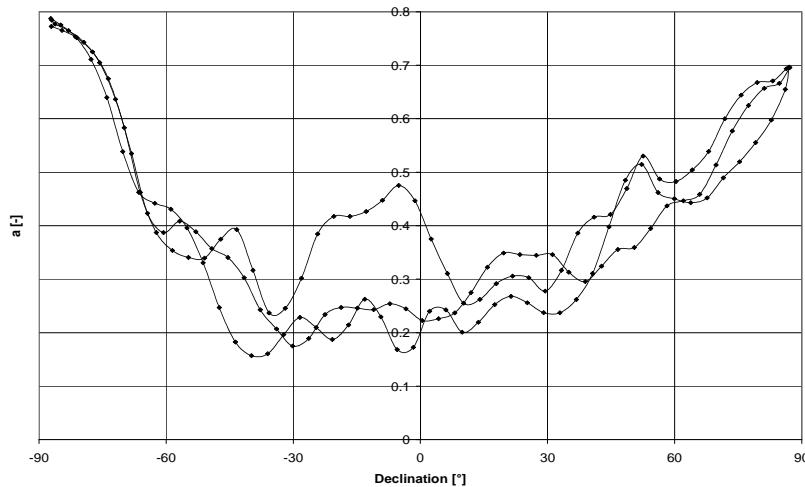
Transient Temperature Computations with the thermal model include:

- Eclipse/ no eclipse phases
- Fluctuation of external heat loads vs. declination (data from CHAMP mission adapted to the GOCE orbit)
- Time dependency of unit power dissipation
- Thrust Profile
- Atmospheric Heating

Seite 11

## GOCE - Thermo-Elastic Distortion Analysis

### Mechanical and Thermal Model and Analysis

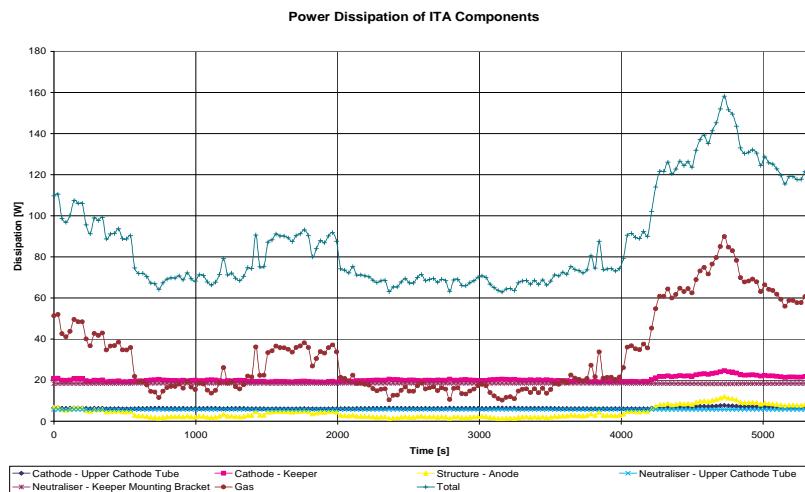


Albedo Factor vs. Declination [deg.]

Seite 12

# GOCE - Thermo-Elastic Distortion Analysis

## Mechanical and Thermal Model and Analysis

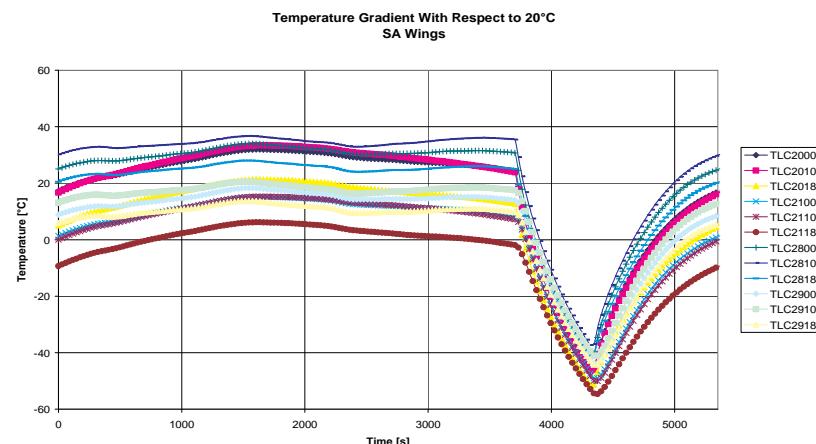


Ion Thruster Power Dissipation [W] per Orbit

Seite 13

# GOCE - Thermo-Elastic Distortion Analysis

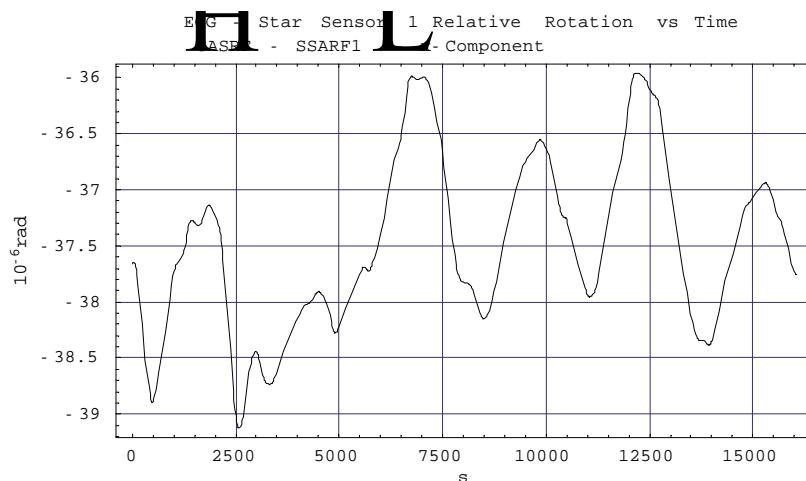
## Mechanical and Thermal Model and Analysis



Temperatures for Thermal Areas on Wing [°C]

Seite 14

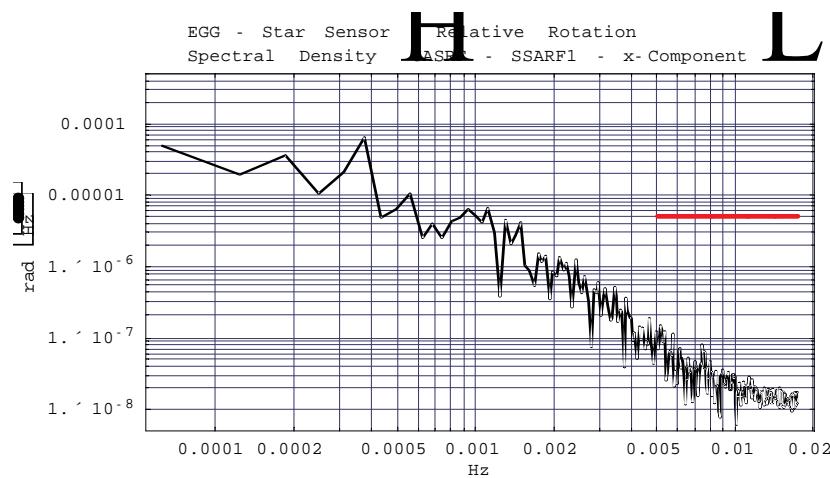
## GOCE - Thermo-Elastic Distortion Analysis Results



Alignment (Relative Rotation) Hot Case (no Eclipse)

Seite 15

## GOCE - Thermo-Elastic Distortion Analysis Results

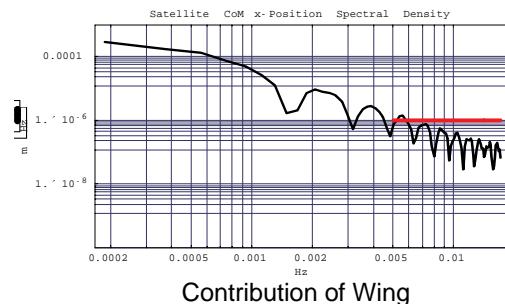
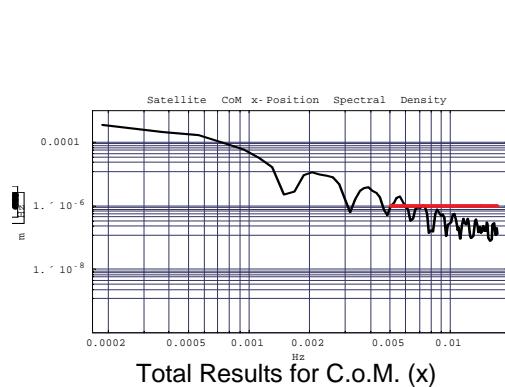


Alignment (Relative Rotation) Spectral Density Hot Case (no Eclipse)

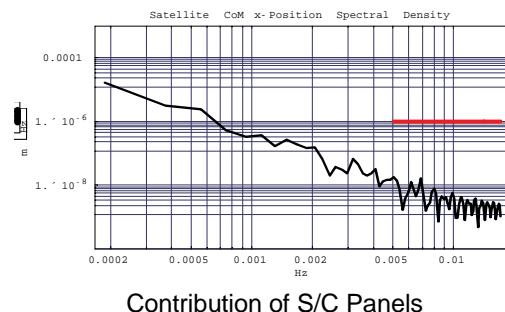
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# GOCE - Thermo-Elastic Distortion Analysis

## Results



Influence of S/C Components on Total Results



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# GOCE - Thermo-Elastic Distortion Analysis

## Summary



### → Experiences with GOCE PFM analysis approach:

- Fast and reliable check if requirements are met with high accuracy
- Easy to vary parameters and to conduct sensitivity analyses
- Quick configuration checks and determination of influence of individual components on the overall results
- No re-run of FEM required for new thermal load cases

### → Suggestions for (Software) Improvements:

ESATAN – functionality for processing thermo-elastic distortion relevant data → routines to read 'unit load case results', generate distortion vs. time output (, compute spectral density)

ESARAD – more detailed planet models required → real earth temperature and albedo factor depend on orbit position/ declination

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# GOCE - Thermo-Elastic Distortion Analysis



## Annex

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# GOCE - Thermo-Elastic Distortion Analysis

## GOCE Mission - Orbit and Load Cases



### Main Orbit Parameters:

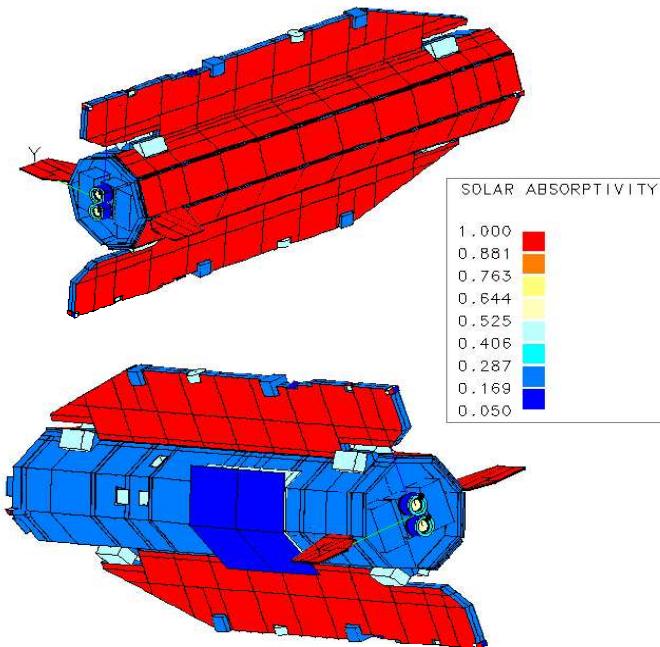
- dawn-dusk or dusk-dawn
- orbit height 240 – 270km
- inclination 96.5°

Case#	HOT-CASE#	COLD-CASE#
LST-Ascending-Nodes#	18:00h	6:00h
Thermo-optical-Properties#	EOL	BOL
Earth-IR-Flux [W/m <sup>2</sup> ]#	261 (average)	189 (average)
Albedo-Coefficient#	0.4 (average)	0.2 (average)
Altitude [km]#	240	250
Inclination [deg]#	96.5	96.5
Solar-Constant [W/m <sup>2</sup> ]#	1408	1323
Solar-Declination [deg]#	-13.00	23.45
Beta-Angle [deg]#	83.5	73.05
Eclipse-Duration [min]#	0	10
Ω-Angle [deg]#	90-deg	270-deg
Attitude#	nominal	nominal
Unit-dissipations#	Max-(EOL)	Min-(BOL)
Heaters#	Enabled	Enabled

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## GOCE - Thermo-Elastic Distortion Analysis

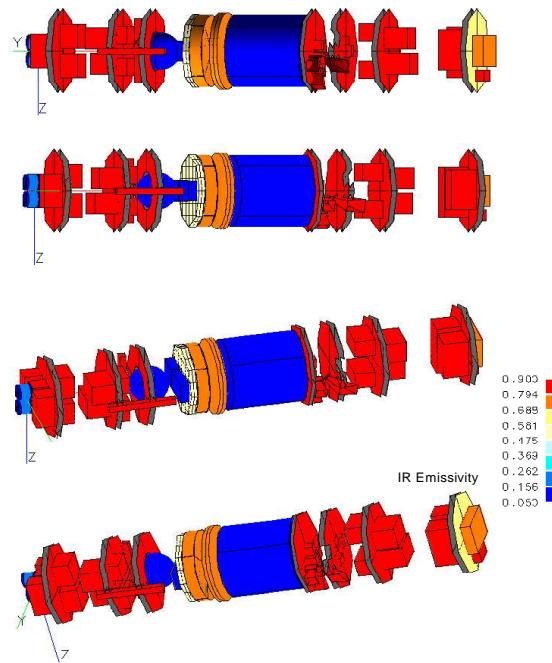
### GOCE Mission - Configuration 1



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## GOCE - Thermo-Elastic Distortion Analysis

### GOCE Mission - Configuration 2



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# GOCE - Thermo-Elastic Distortion Analysis

## Mechanical and Thermal Model and Analysis

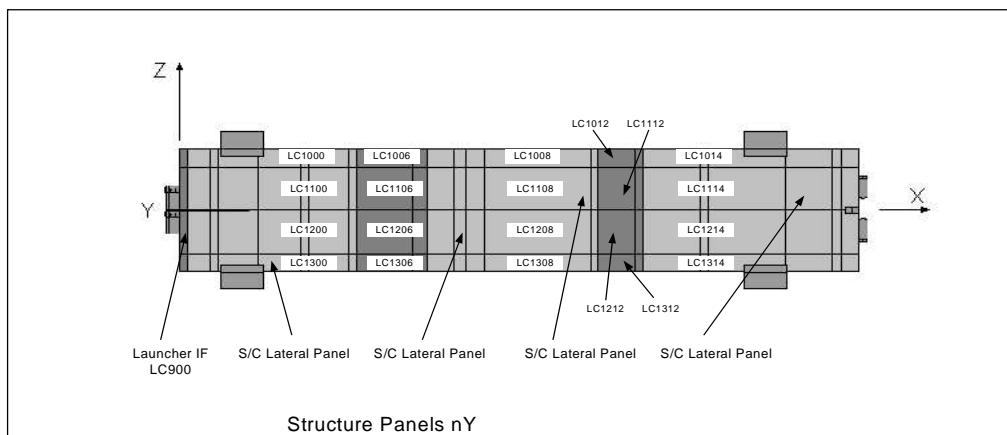
Unit load case count		1	2	3	4
Unit load case no.		900	940	1000	1006
Unit load case description	Basic	Launcher I/F Ring	Launcher I/F Ring	S/C Lateral Panel +Z -Y	S/C Lateral Panel +Z -Y
axi(+x) [m/s^2]	5.2244433632E-09	5.2244437744E-09	5.2244440763E-09	5.2244433262E-09	5.2244431264E-09
axi(-x) [m/s^2]	-6.1323390129E-09	-6.1323382266E-09	-6.1323375849E-09	-6.1323391596E-09	-6.1323390082E-09
ayi(+y) [m/s^2]	-6.7900107660E-09	-6.7900110939E-09	-6.7900097959E-09	-6.7900111551E-09	-6.7900113691E-09
ayi(-y) [m/s^2]	-8.1676499037E-10	-8.1676540917E-10	-8.1676442773E-10	-8.1676682072E-10	-8.1676508200E-10
azi(+z) [m/s^2]	-2.5769425791E-09	-2.5769424682E-09	-2.5769425105E-09	-2.5769425775E-09	-2.5769410747E-09
azi(-z) [m/s^2]	1.4633527638E-09	1.4633526648E-09	1.4633525573E-09	1.4633539866E-09	1.4633535272E-09

### Self-Gravity Acceleration Data

Seite 23

# GOCE - Thermo-Elastic Distortion Analysis

## Mechanical and Thermal Model and Analysis

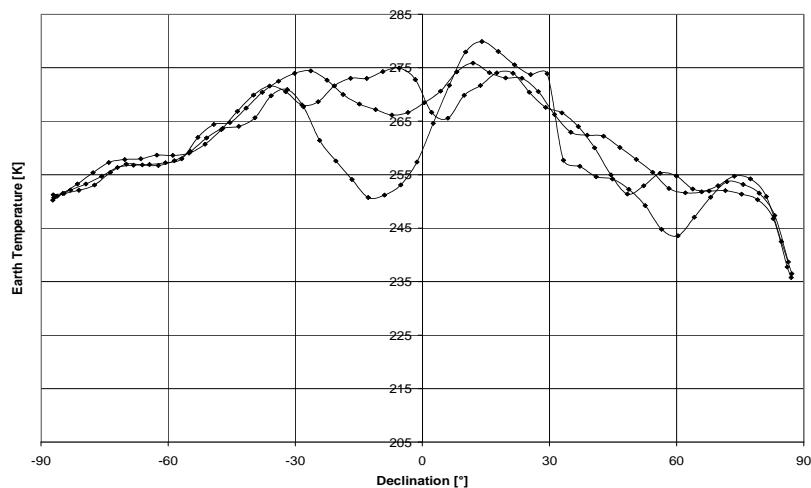


### Example - Thermal Areas → Unit Load Cases

Seite 24

# GOCE - Thermo-Elastic Distortion Analysis

## Mechanical and Thermal Model and Analysis

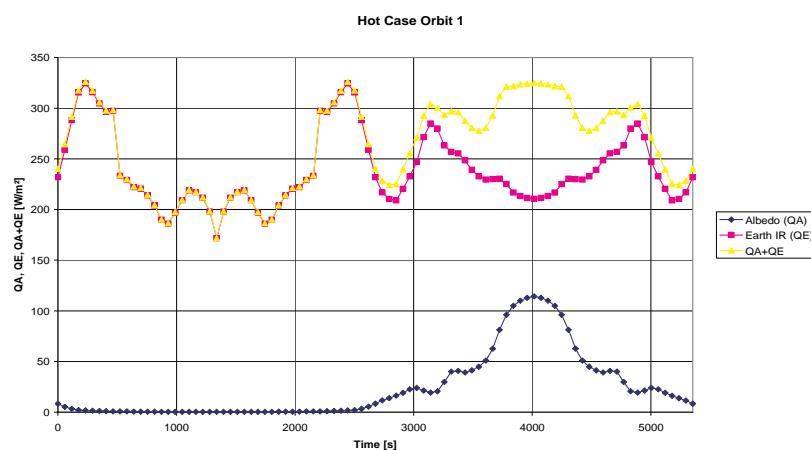


Earth Temperature [K] vs. Declination [deg.]

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# GOCE - Thermo-Elastic Distortion Analysis

## Mechanical and Thermal Model and Analysis



Resulting External Heat Loads [ $\text{W/m}^2$ ] vs. Declination [deg.]

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# GOCE - Thermo-Elastic Distortion Analysis

## Mechanical and Thermal Model and Analysis

```

INTEGER orbit_index;

/* 97 orbit positions = 92 + 1 start=stop at equator + 4 eclipse entry/exit */
REAL ALBEDO_FAC [97] = {
  0.14348174,
  0.13528350,
  0.09871711,
  0.05825458,
  0.03680240,
  ...
  0.13099252,
  0.13296514,
  0.14348174
};

CALCULATE_PLANET_ABSORBED_FLUX_RAYTRACING (
  ir_paf = COLD_BOL_p23p45.IR_PAF[orbit_index],
  coord = COLD_BOL_p23p45.ORBIT_POSITIONS[orbit_index],
  albedo_paf = COLD_BOL_p23p45.ALBEDO_PAF[orbit_index],
  planet_rad = COLD_BOL_p23p45.ORBIT.PLANET_RADIUS,
  planet_temp = PLANET_TEMP [orbit_index],
  albedo_reflect_coeff = ALBEDO_FAC [orbit_index],
  solar_char = COLD_BOL_p23p45.SOLAR_CONST_OVERRIDE);

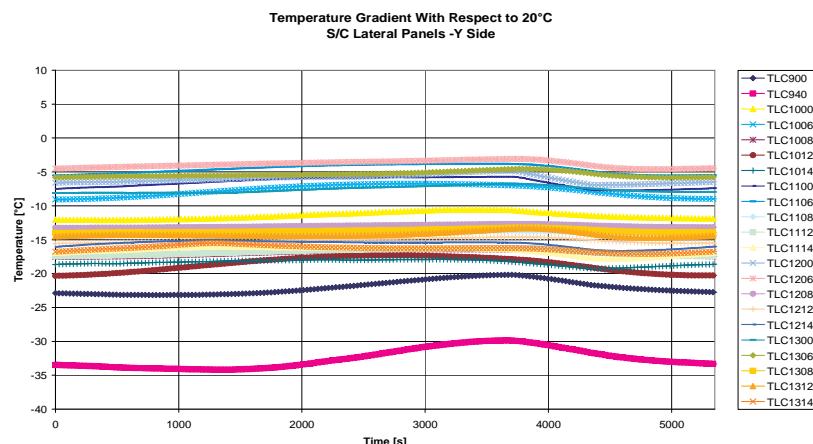
```

ESARAD – example albedo factor

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# GOCE - Thermo-Elastic Distortion Analysis

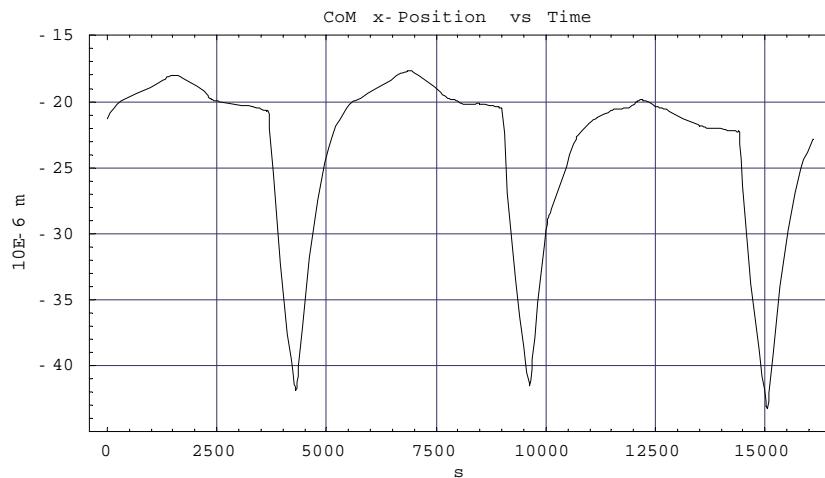
## Mechanical and Thermal Model and Analysis



Temperatures for Thermal Areas on S/C Panels [°C]

Seite 28

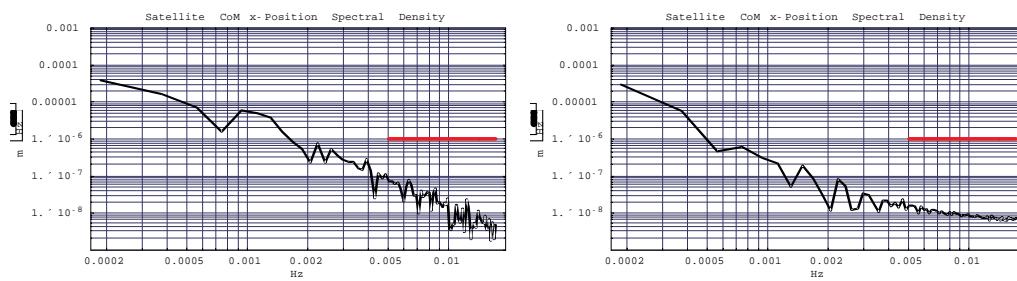
## GOCE - Thermo-Elastic Distortion Analysis Results



C.o.M Position Change Cold Case (Eclipse)

Seite 29

## GOCE - Thermo-Elastic Distortion Analysis Results

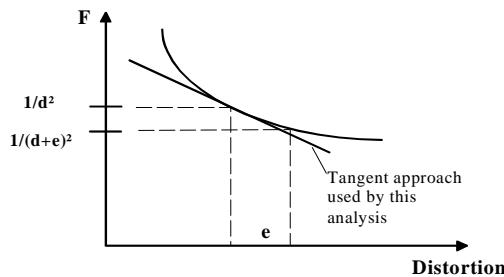


Assessment – Transient vs. Constant External Heat Loads and Unit Power Dissipation

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## GOCE - Thermo-Elastic Distortion Analysis

### Linearization Error

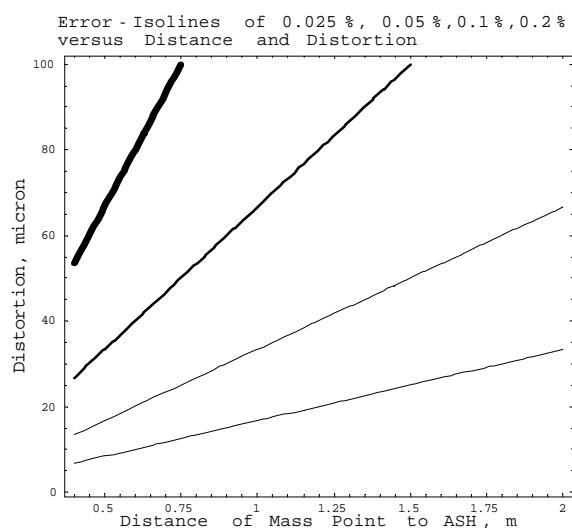


- linearization error is given by the thermal unit load cases
- the gravity potential  $d$  is non-linear
- error by multiplying the unit load case result by the actual temperature swing
- error is negligibly small as long as the distortions are in the range of only a few microns and the distance of the mass points are larger than 0.5 m

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## GOCE - Thermo-Elastic Distortion Analysis

### Linearization Error



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